



Introduction to Neutrinos and Neutrino Oscillations

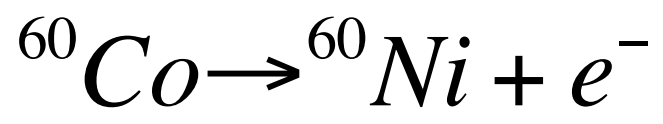
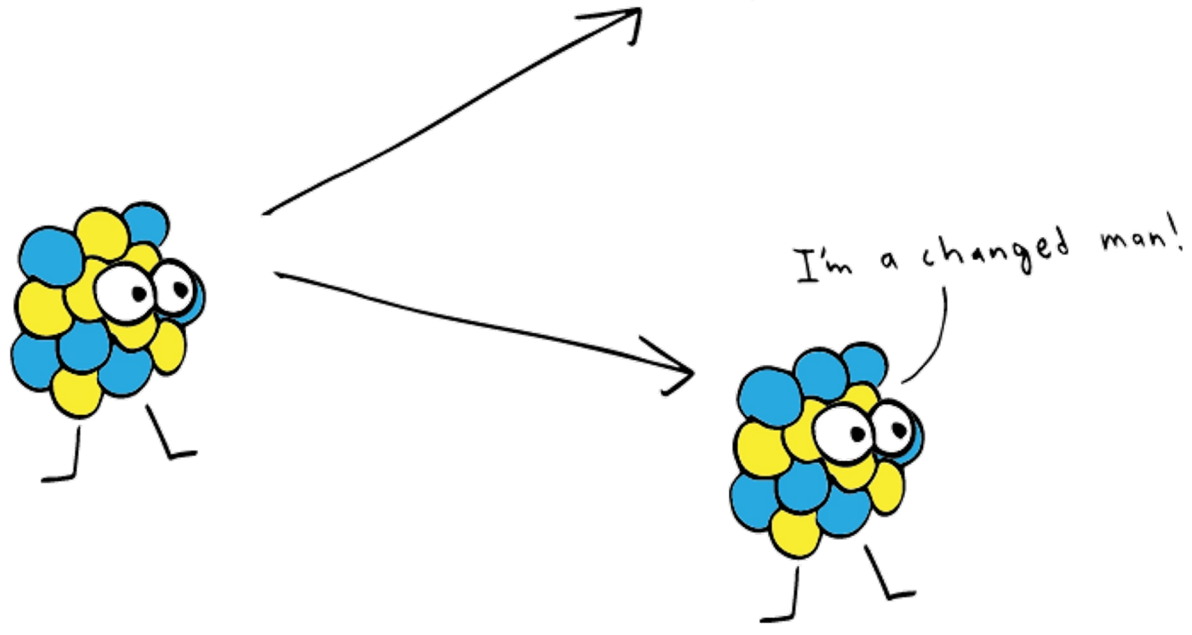
Alex Himmel



2024 Neutrino University
June 26th, 2024

Beta Decay

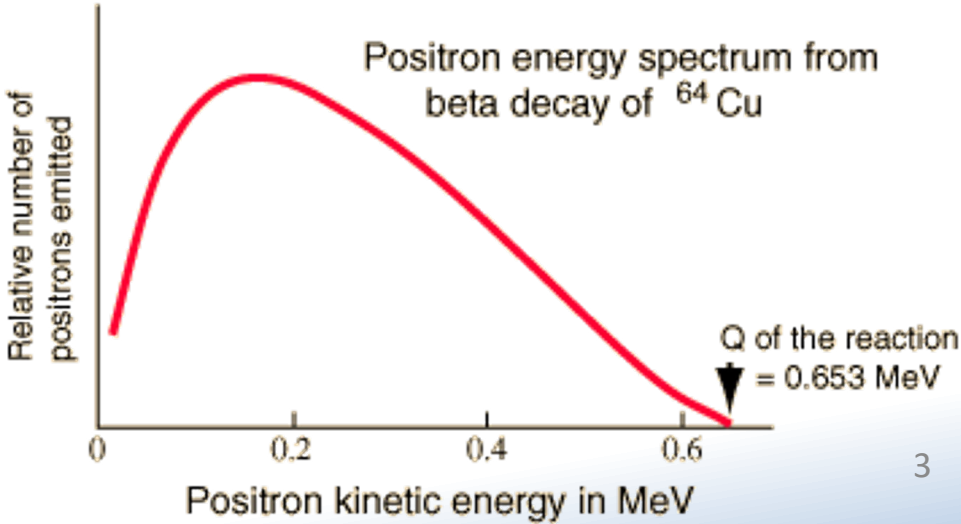
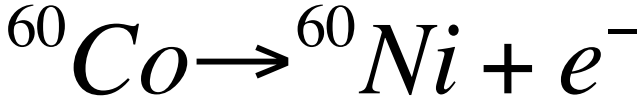
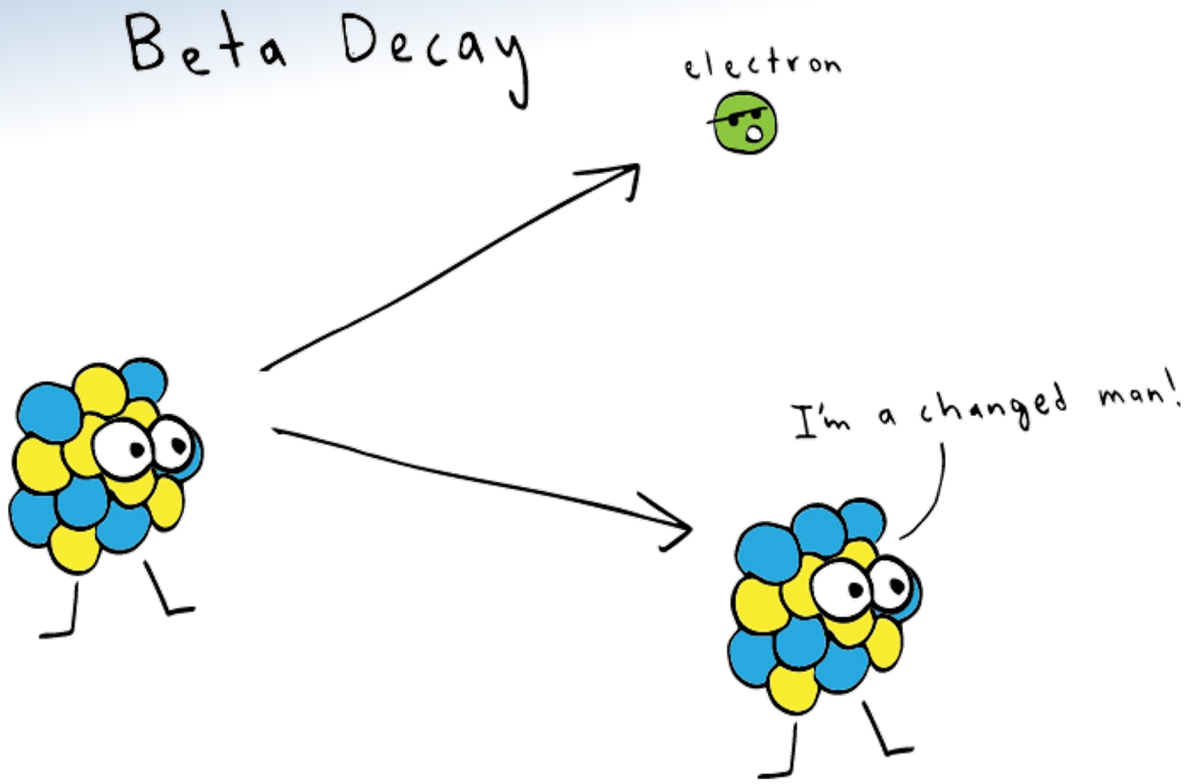
electron

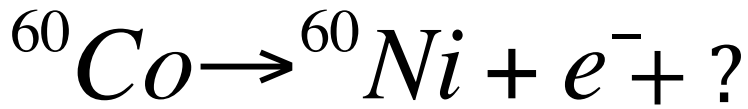
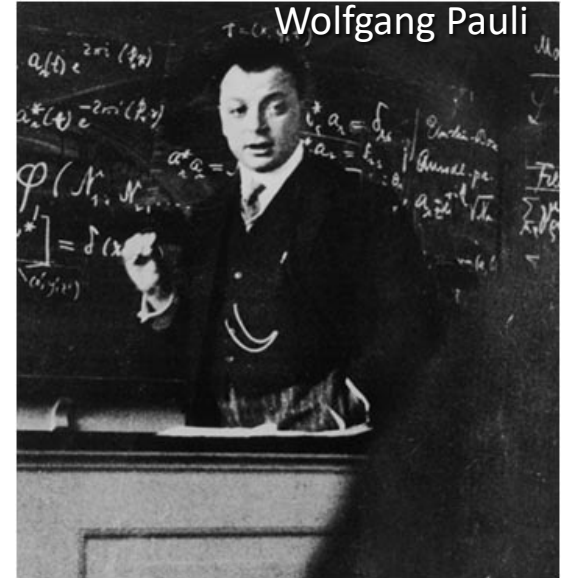
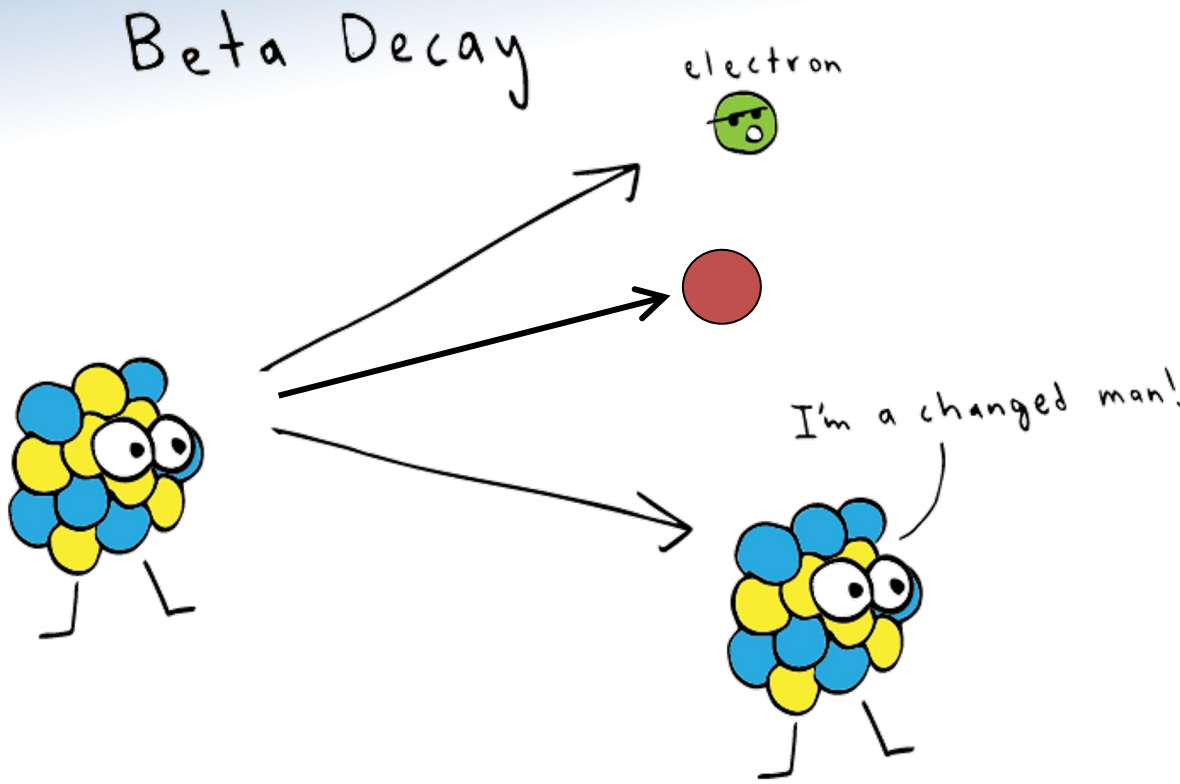
1913



1913



1930



Physikalisches Institut
der Eidg. Technischen Hochschule
Zürich

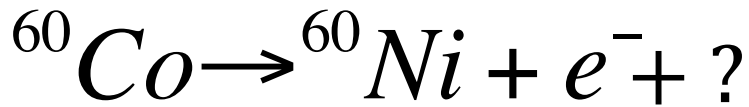
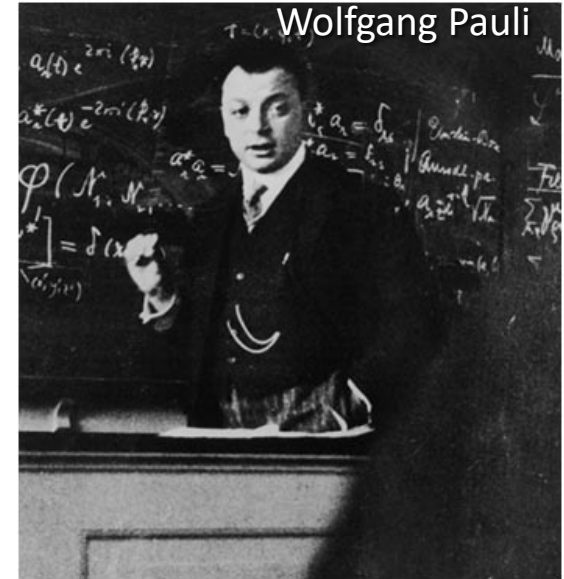
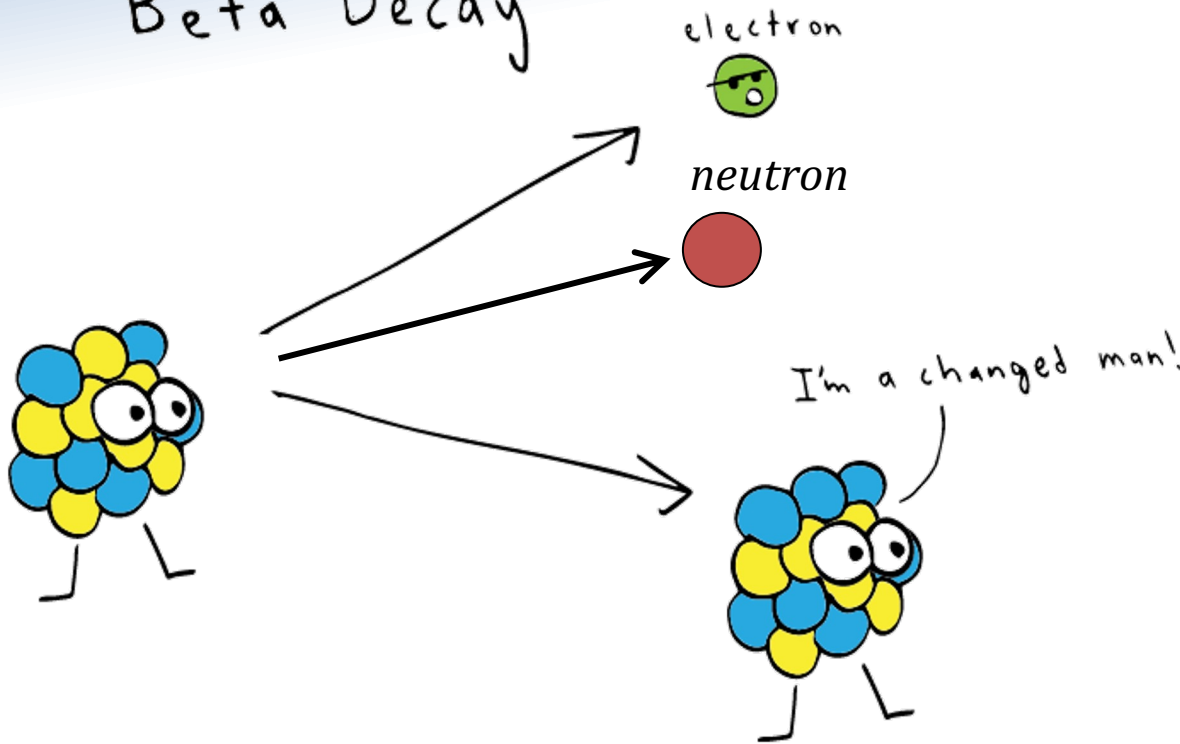
Zürich, 4. Dez. 1930
Gloriastrasse

Liebe Radioaktive Damen und Herren,

Wie der Ueberbringer dieser Zeilen, den ich huldvollst
anzuhören bitte, Ihnen des näheren auseinandersetzen wird, bin ich

1930

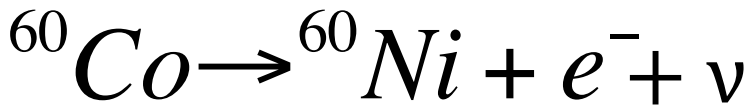
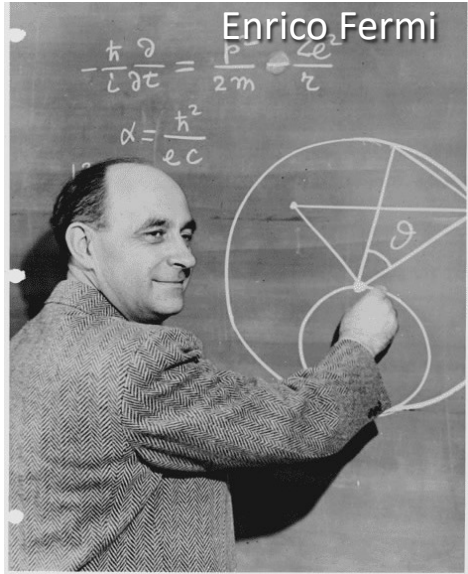
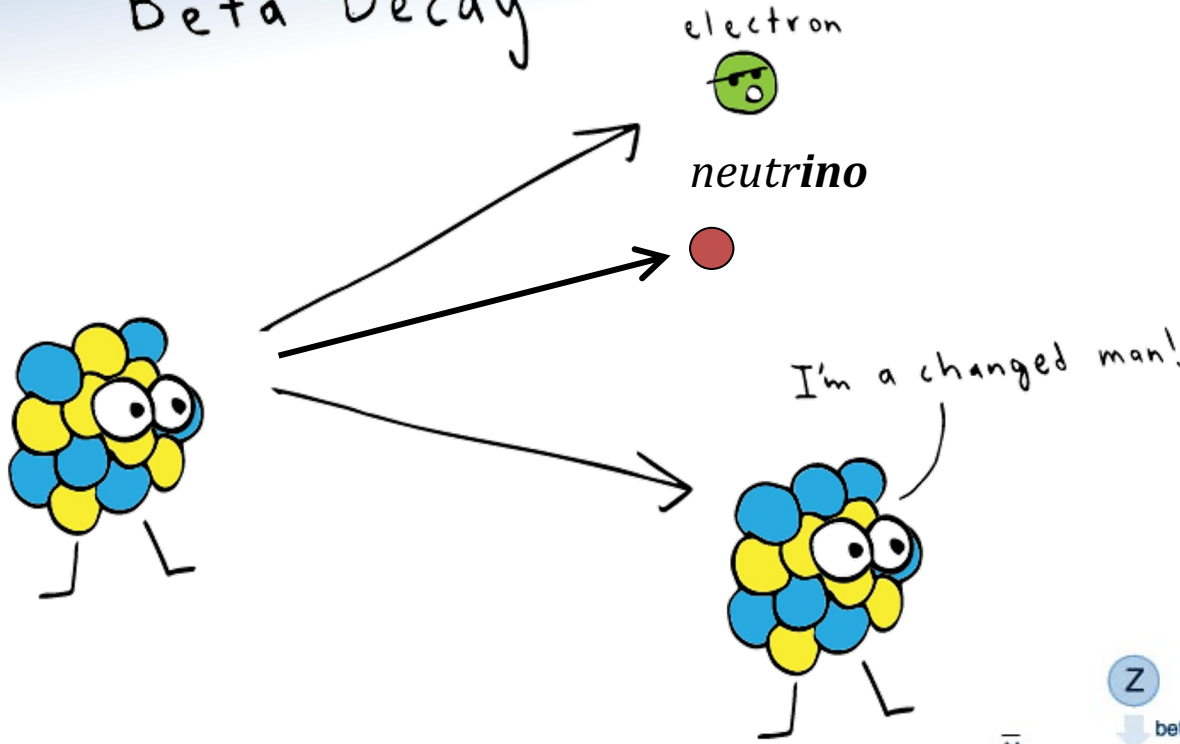
Beta Decay



beta-Zerfall mit dem Elektron jeweils noch ein Neutron emittiert wird, derart, dass die Summe der Energien von Neutron und Elektron konstant ist.

1933

Beta Decay



Fermi's neutrino is massless and feels only the weak force

beta decay

Fermi function to account for the nuclear coulomb interaction with the emitted particle.

Shape factor to correct the matrix element for various types of "forbidden" decay paths.

$$N(p) = Cp^2(Q - KE_e)^2 F(Z', p) |M_{fi}|^2 S(p, q)$$

Distribution of electron momentum

Statistical factor derived from the density of final states available to the emitted particles.

Matrix element for allowed transitions gives the strength of the interaction between initial and final states.

Electron kinetic energy

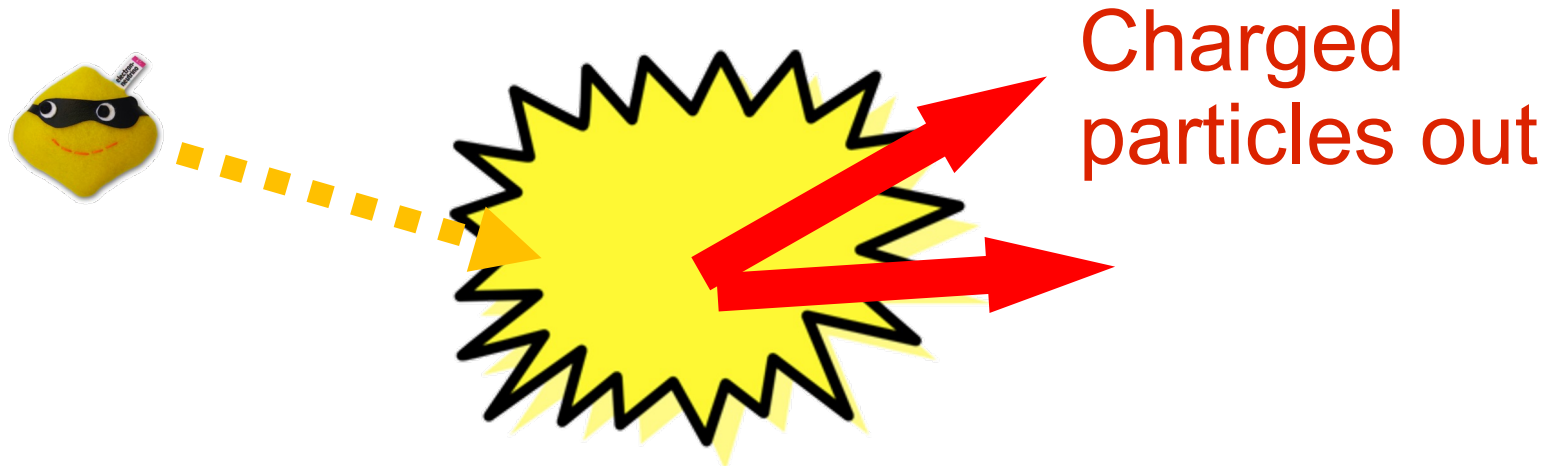
Electron momentum

How to “See” a Neutrino



- Neutrinos, being neutral, do not interact with photons. They are *literally* invisible.

How to “See” a Neutrino



- Neutrinos, being neutral, do not interact with photons. They are *literally* invisible.
- When the neutrino collides with an atom, it produces charged particles.
- They *are* visible and seem to appear out of nowhere.

Only Weak Interactions

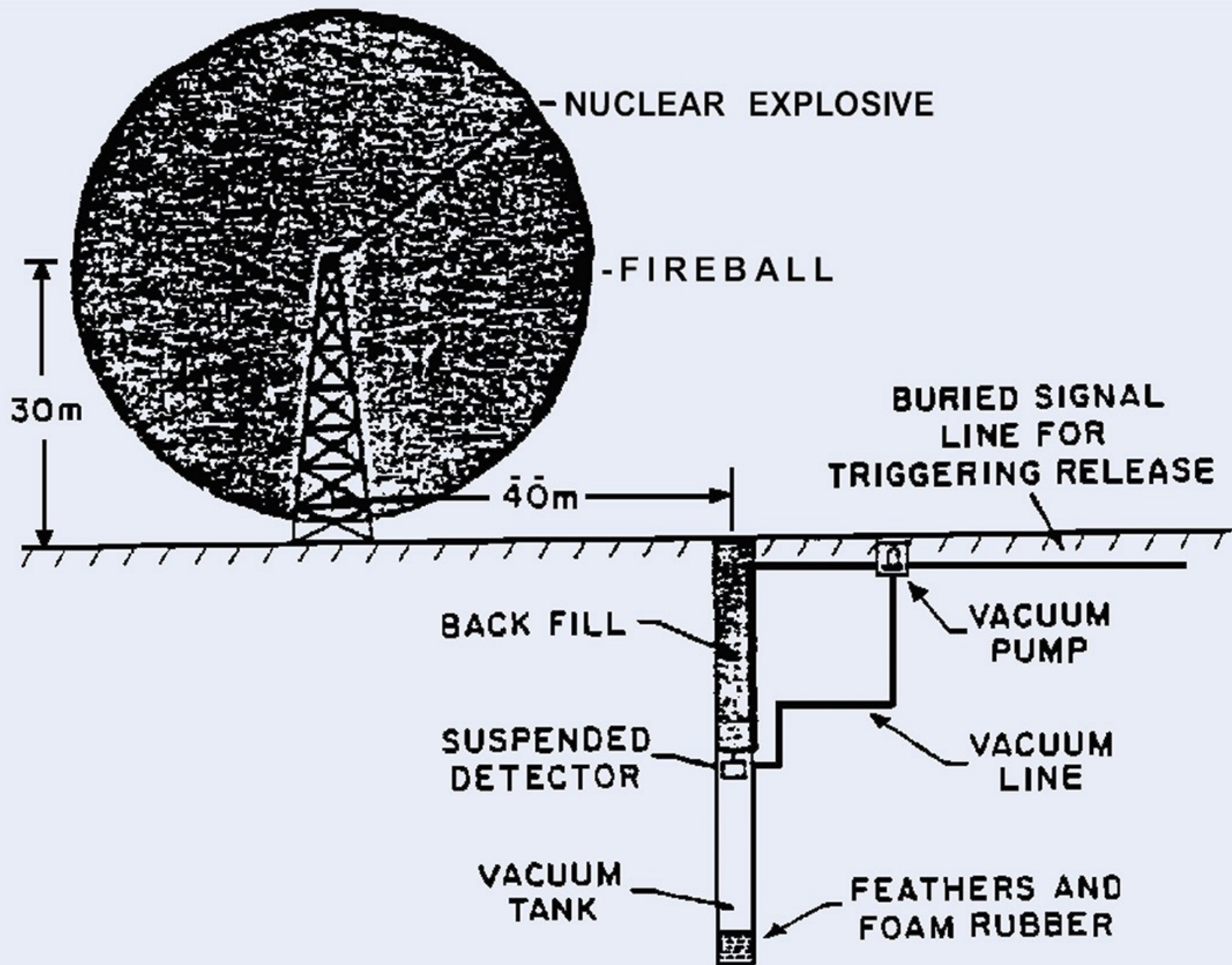
Strength \sim frequency of collisions

Interaction length for a high-energy photon in carbon is **~ 20 cm.**



For a neutrino of the same energy its **~ 1 light year!**

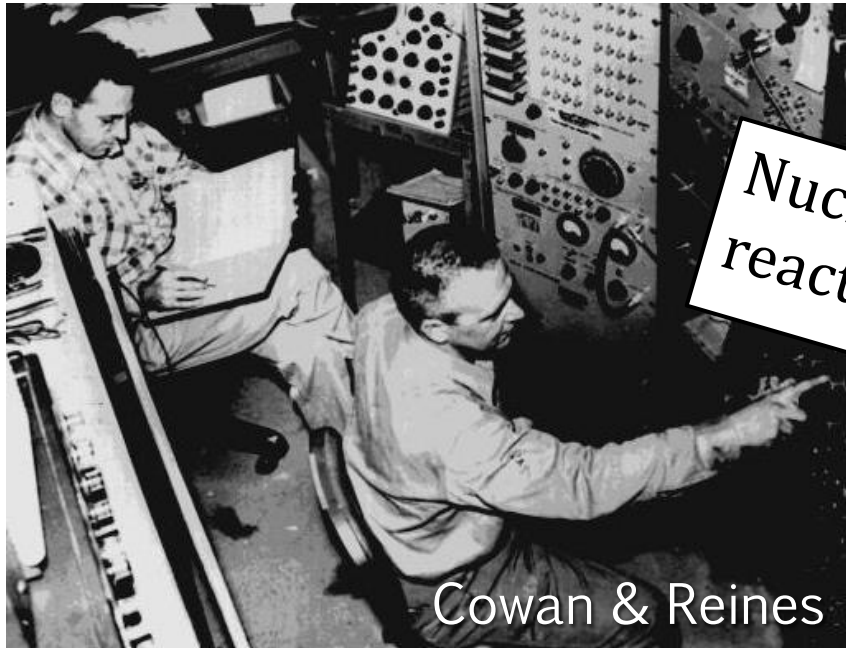
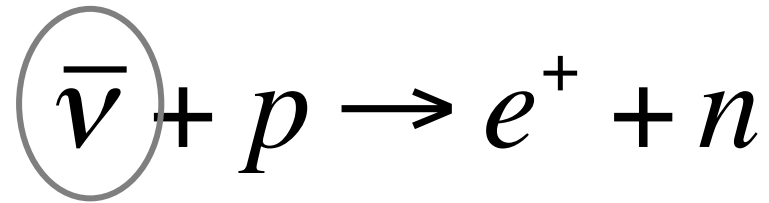




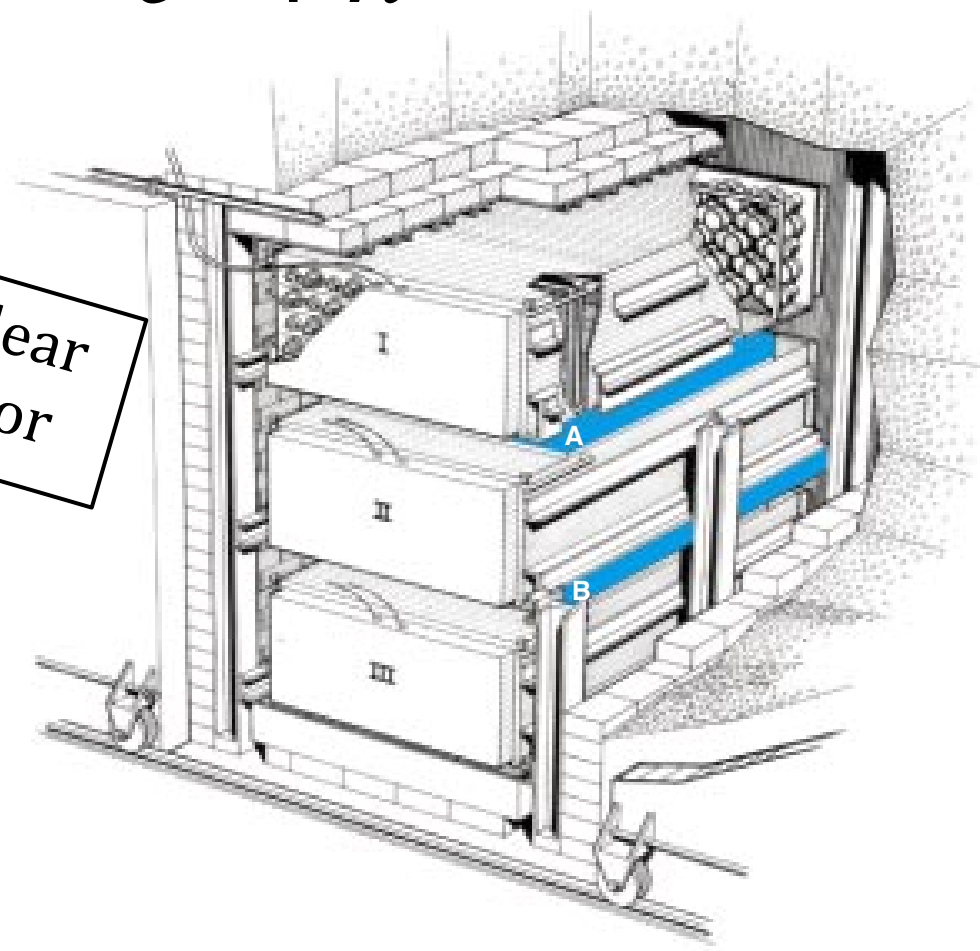
The First Detection

1956

Invisible



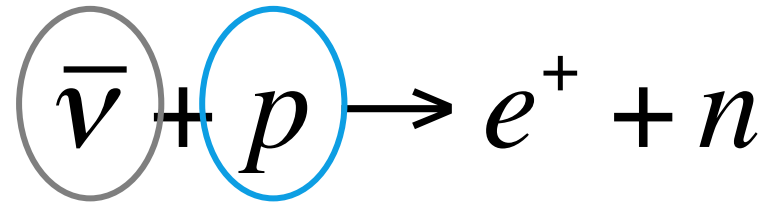
Nuclear reactor



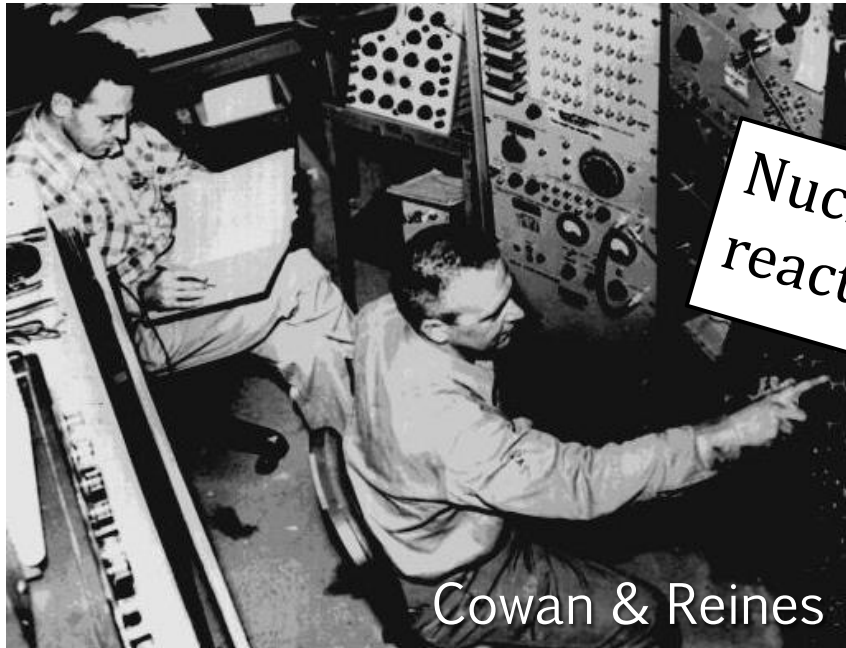
The First Detection

1956

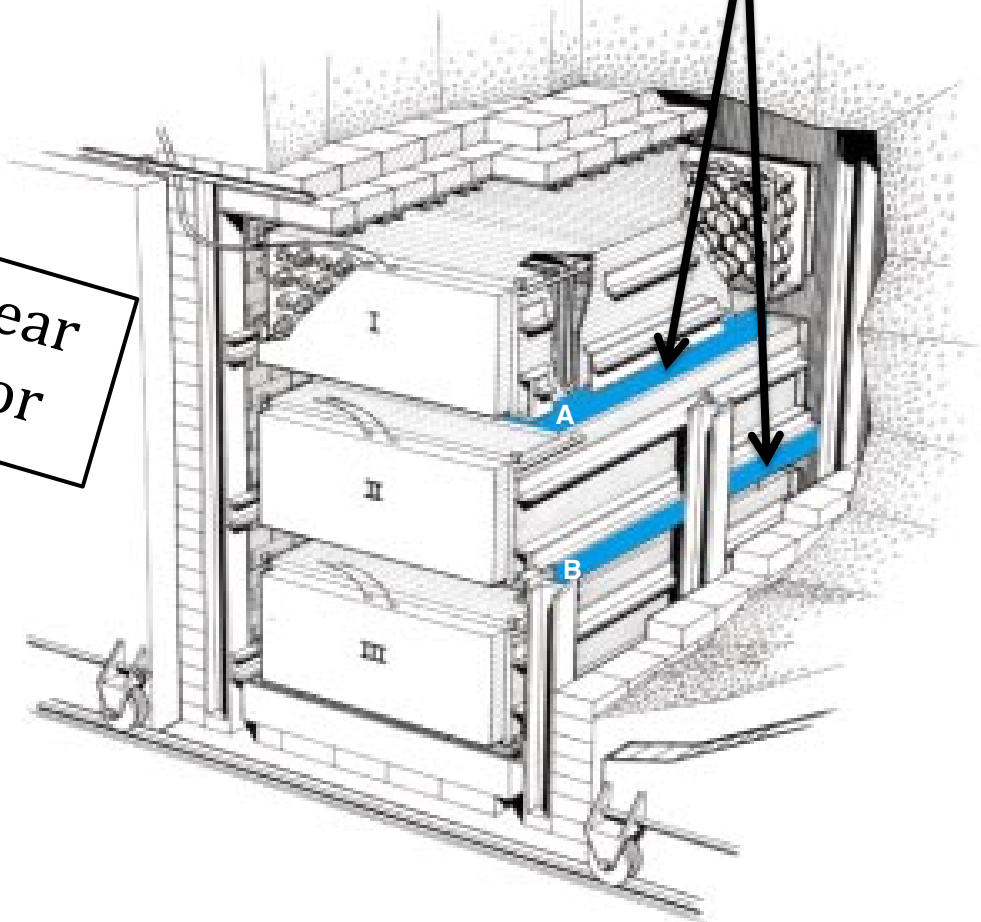
Invisible Hydrogen



H₂O + Cd

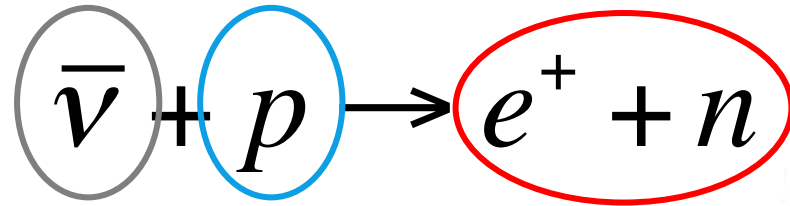


Nuclear reactor



The First Detection

Invisible Hydrogen



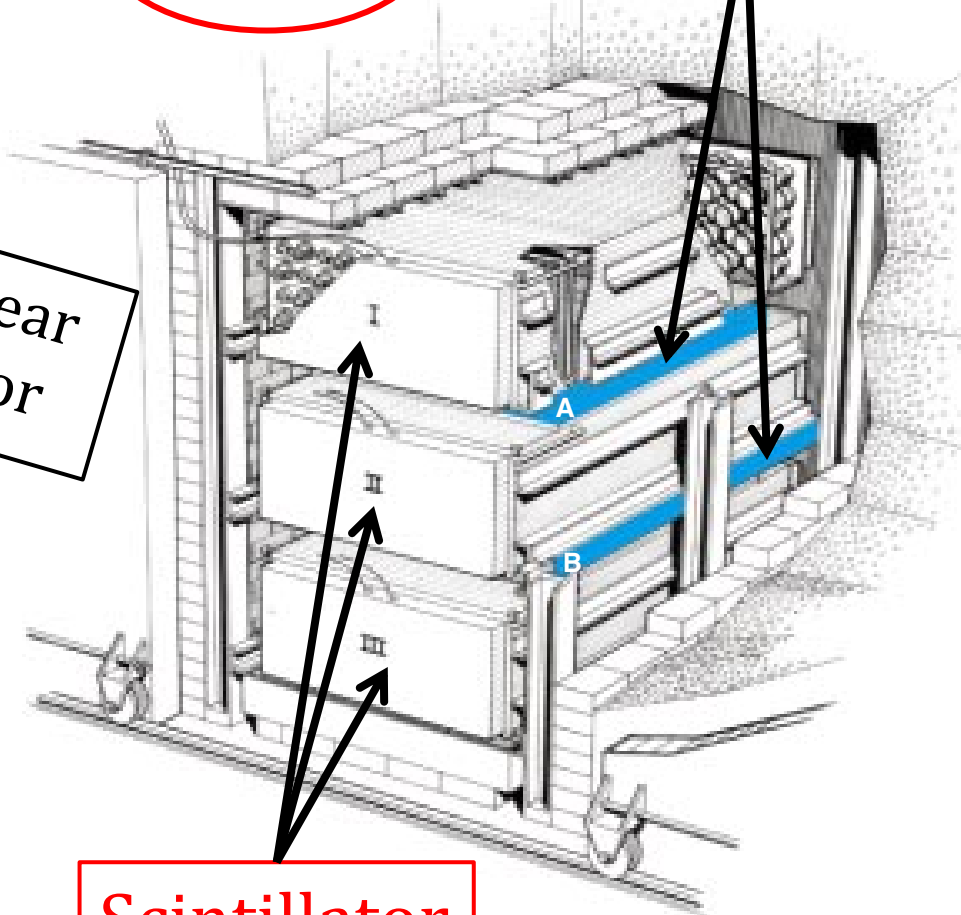
Produce light in Scintillator

1956

H₂O + Cd



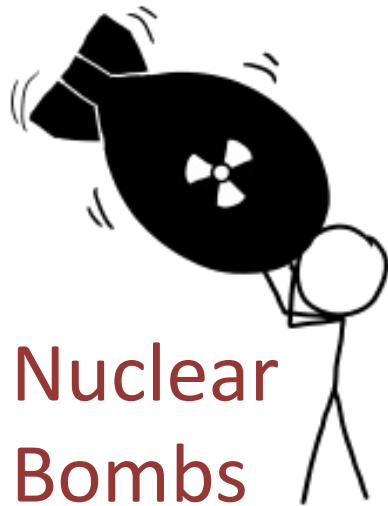
Nuclear reactor



Scintillator

Where do neutrinos come from?

Reactors

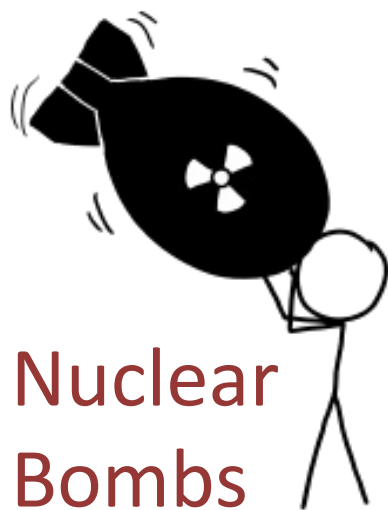


Nuclear Bombs

<https://what-if.xkcd.com/73/>

Where do neutrinos come from?

Reactors



Nuclear Bombs

<https://what-if.xkcd.com/73/>

Accelerators



Discovery of Neutrino Flavor

1962

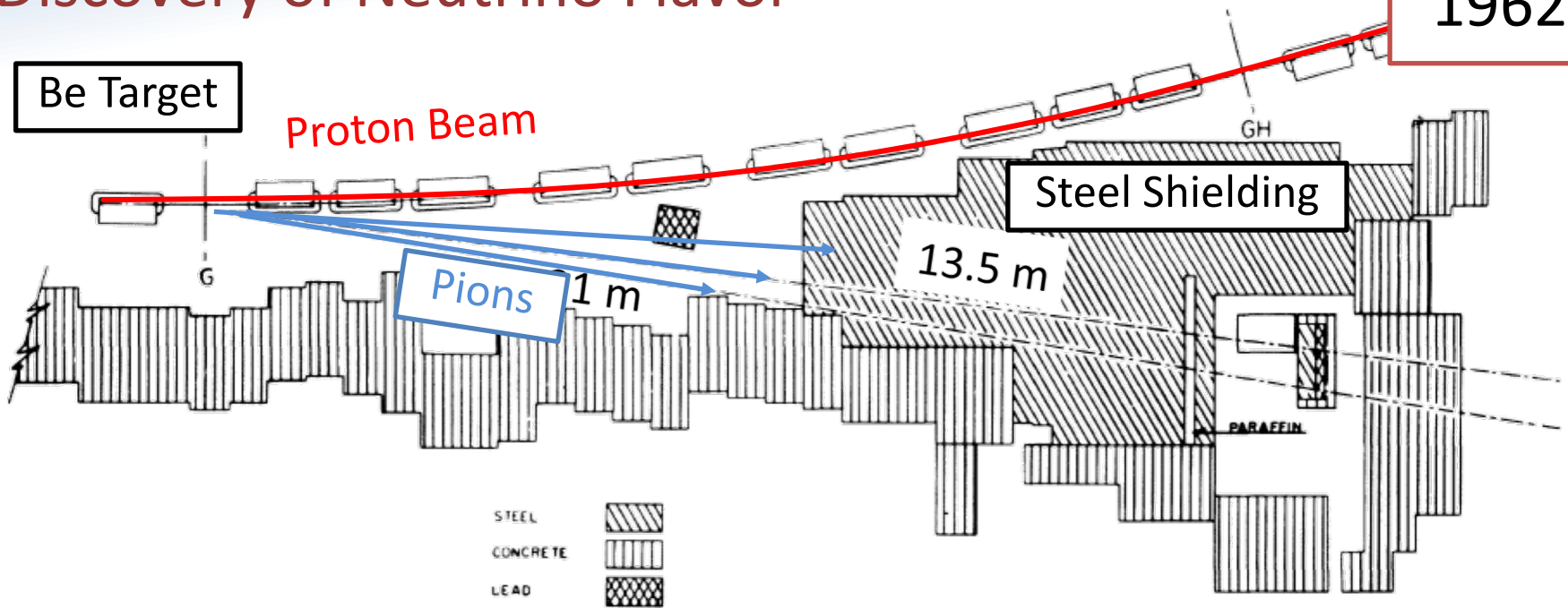
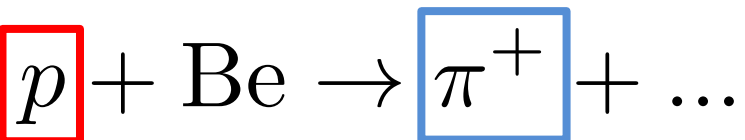


FIG. 1. Plan view of AGS neutrino experiment.



Discovery of Neutrino Flavor

1962

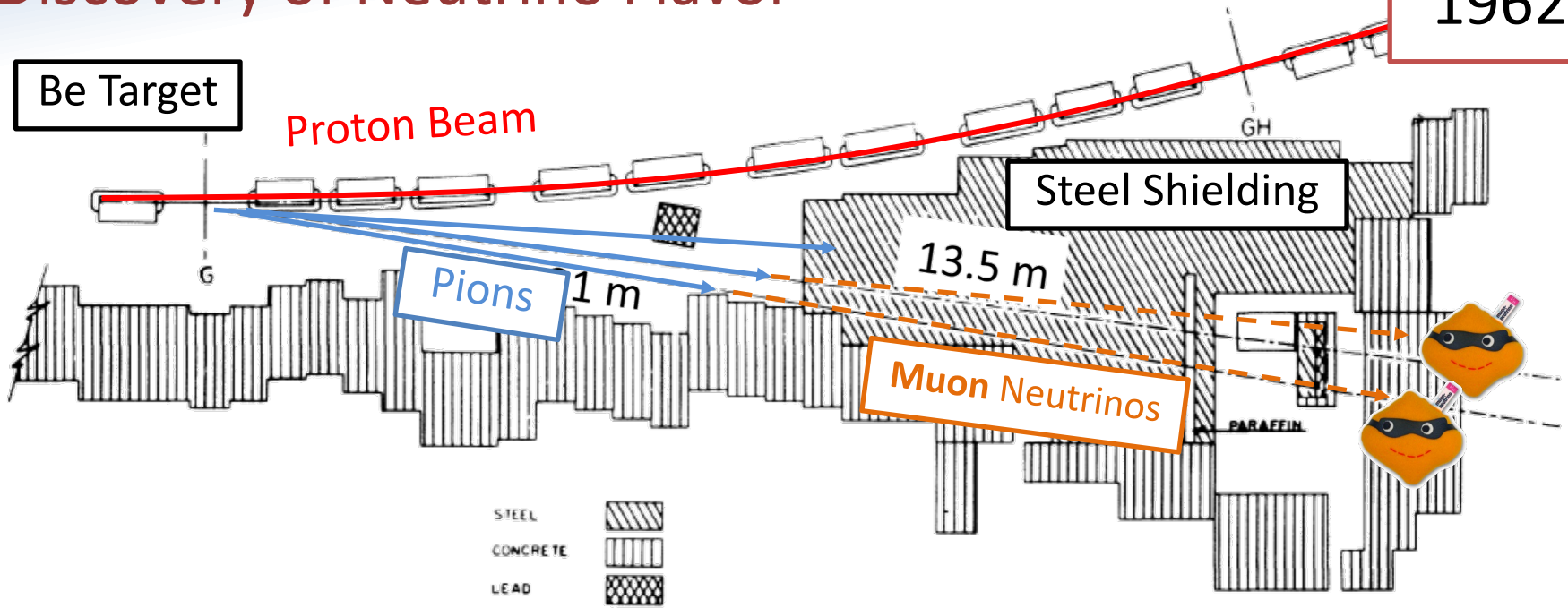
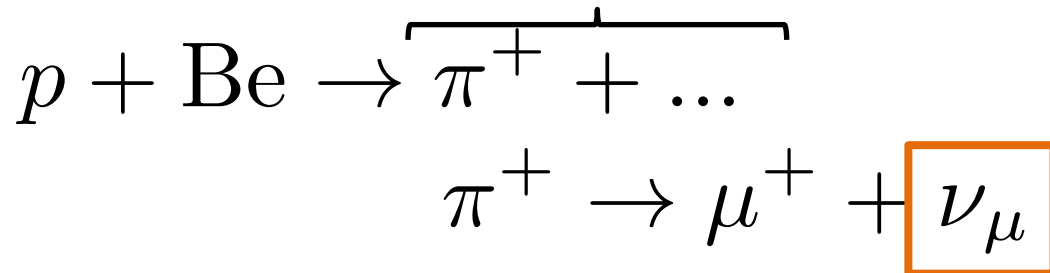


FIG. 1. Plan view of AGS neutrino experiment.

Stopped by
steel shielding



Discovery of Neutrino Flavor

1962

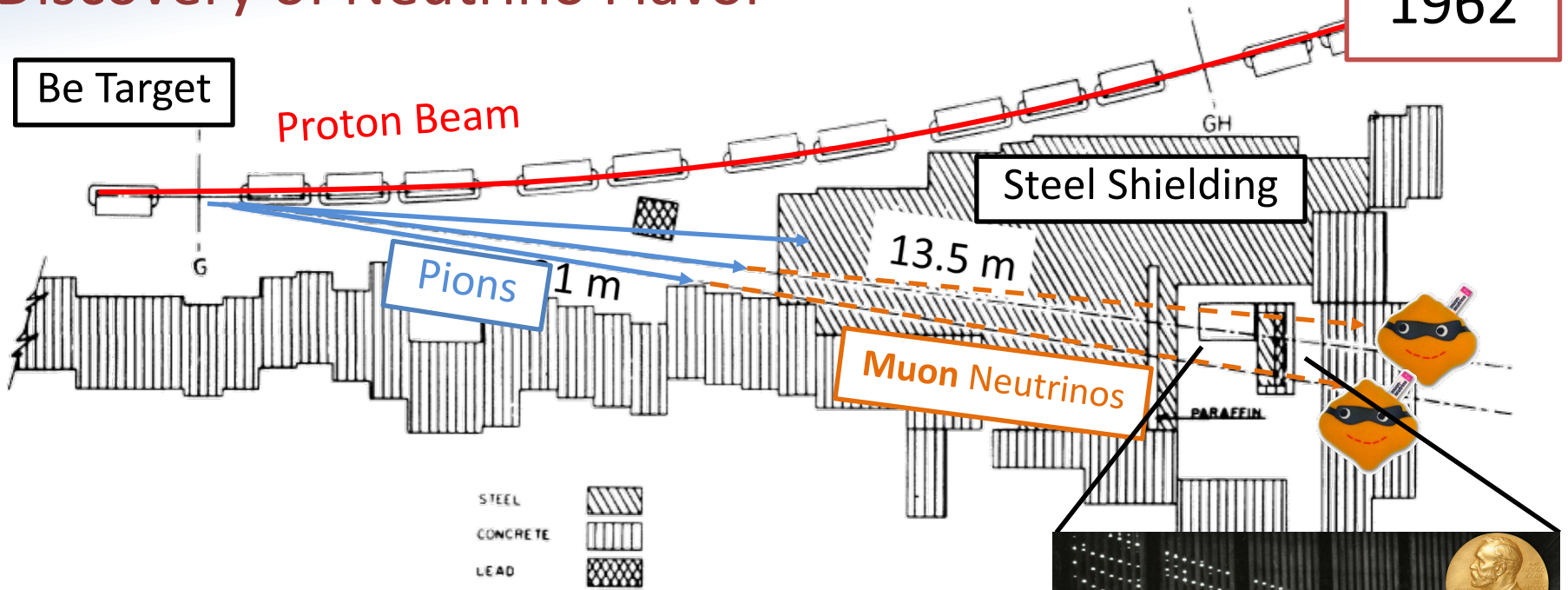
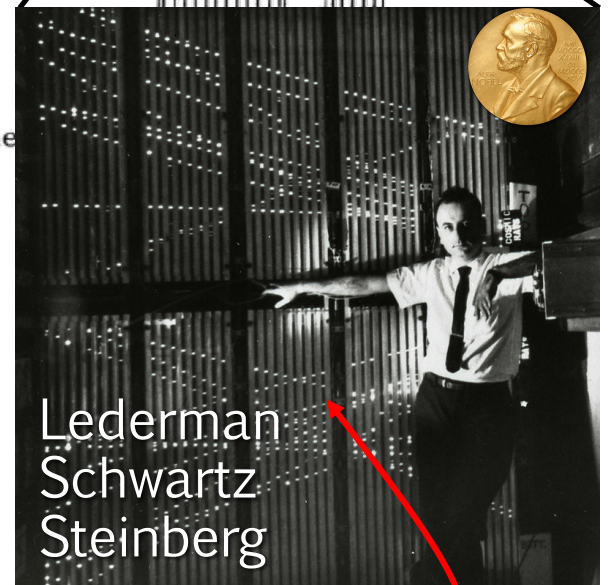
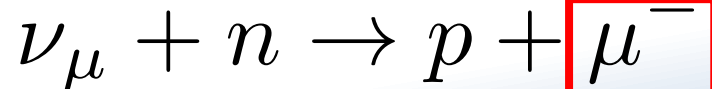
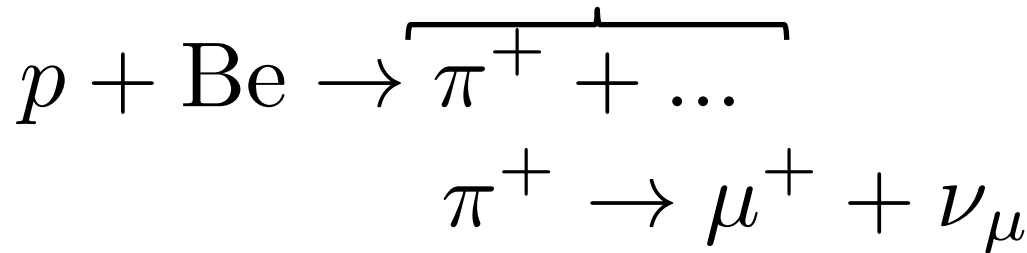


FIG. 1. Plan view of AGS neutrino experiment

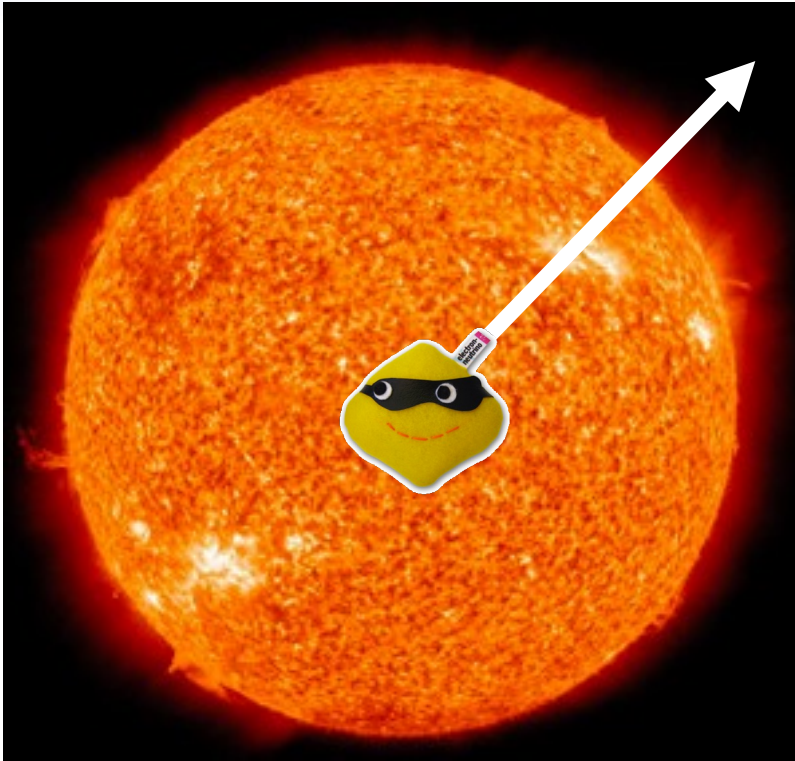


Lederman
Schwartz
Steinberg

Stopped by
steel shielding

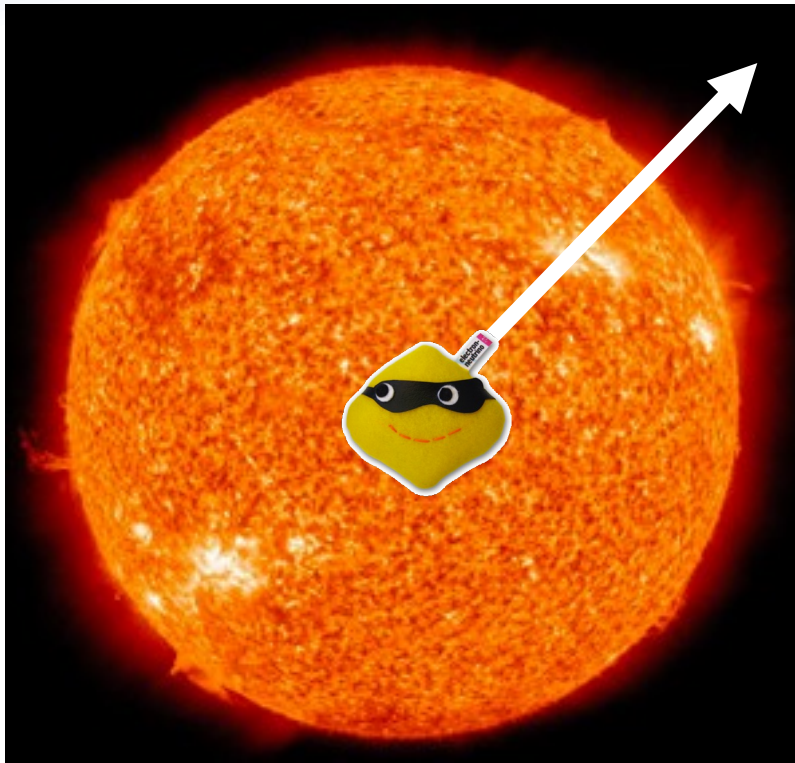


Solar Neutrinos

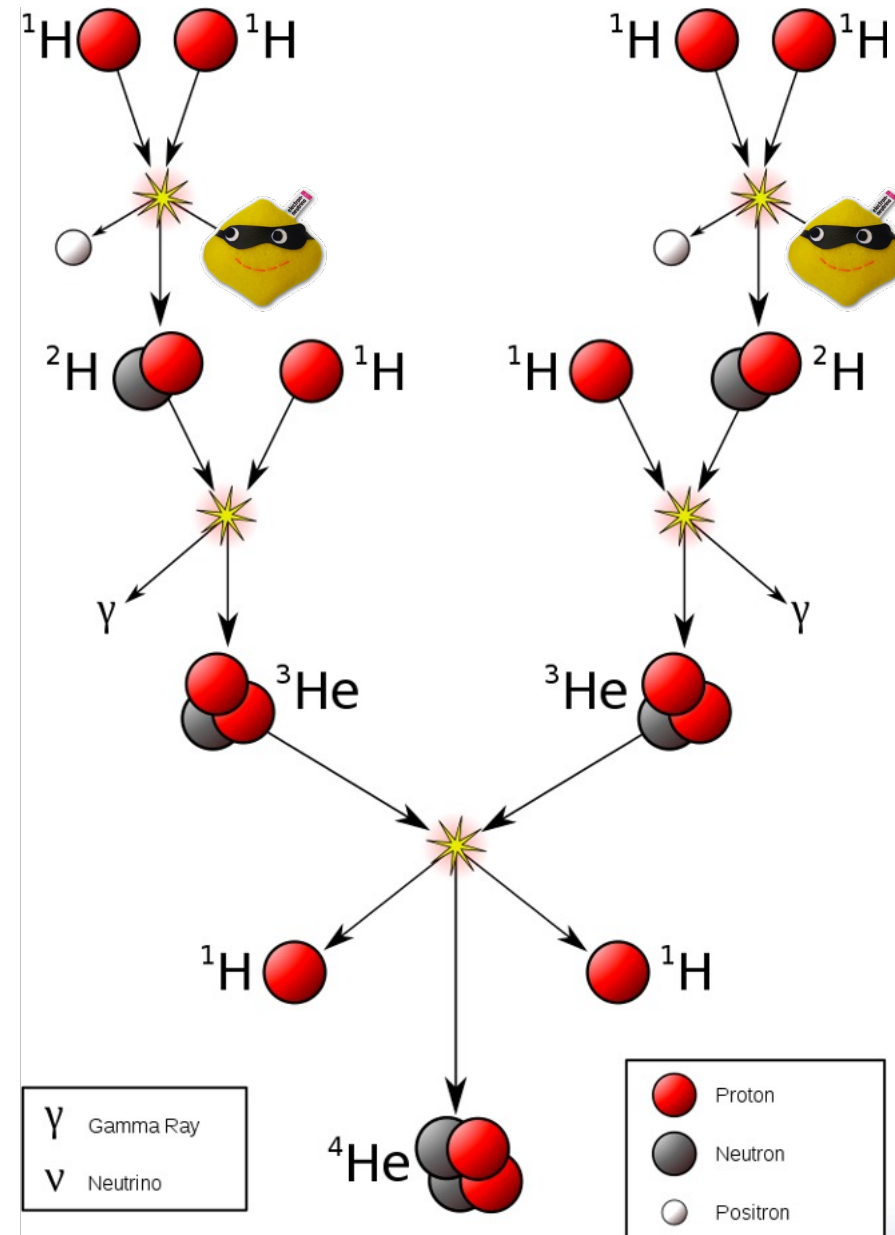


- Blessing of weak interactions – carry information from deep inside heavy objects.

Solar Neutrinos

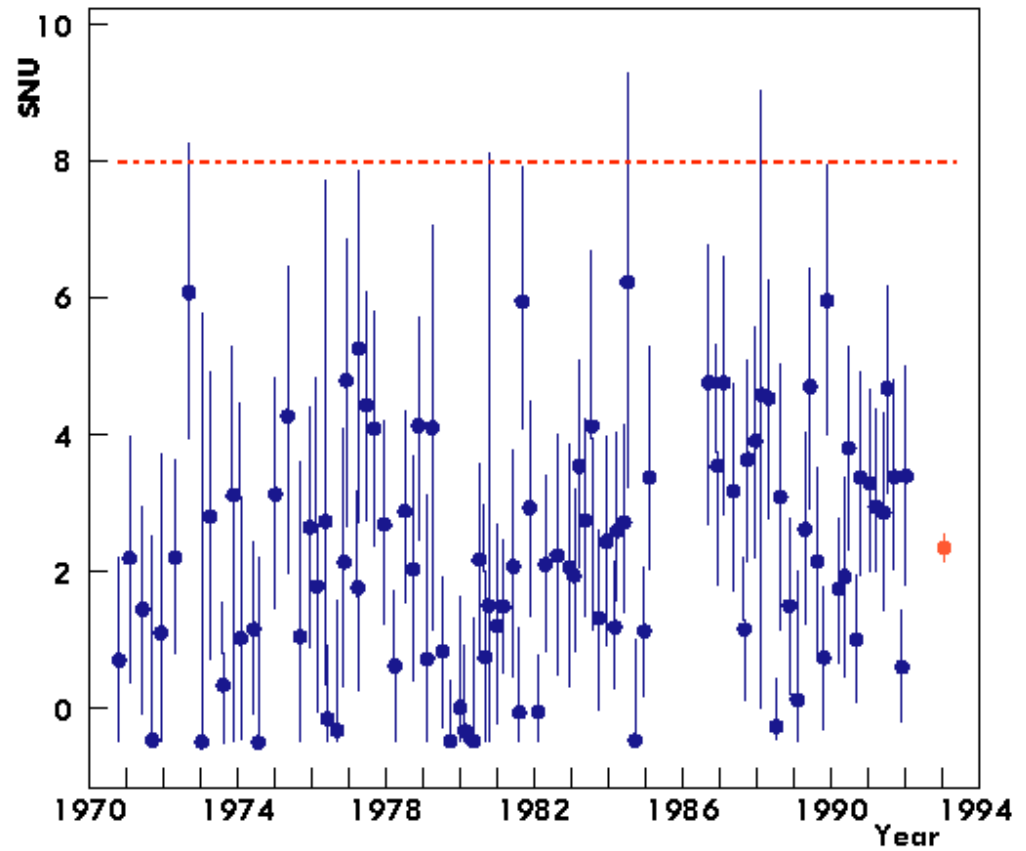
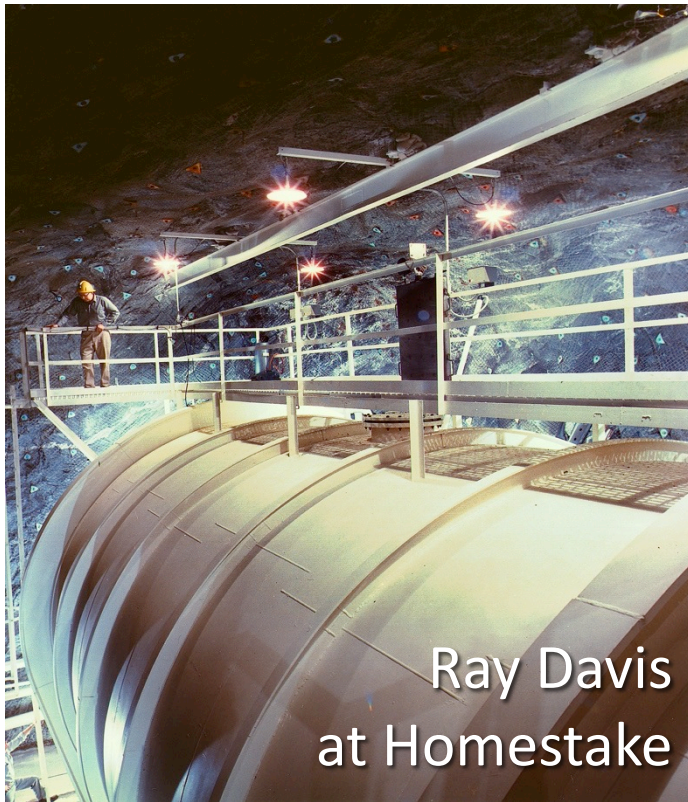
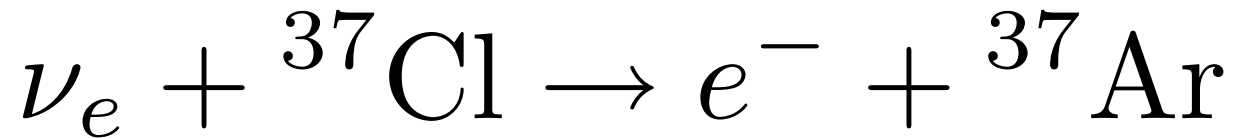


- Blessing of weak interactions – carry information from deep inside heavy objects.
- Rate of neutrinos from fusion is extremely sensitive to the temperature of the sun.



Solar Neutrinos become a Problem

1969

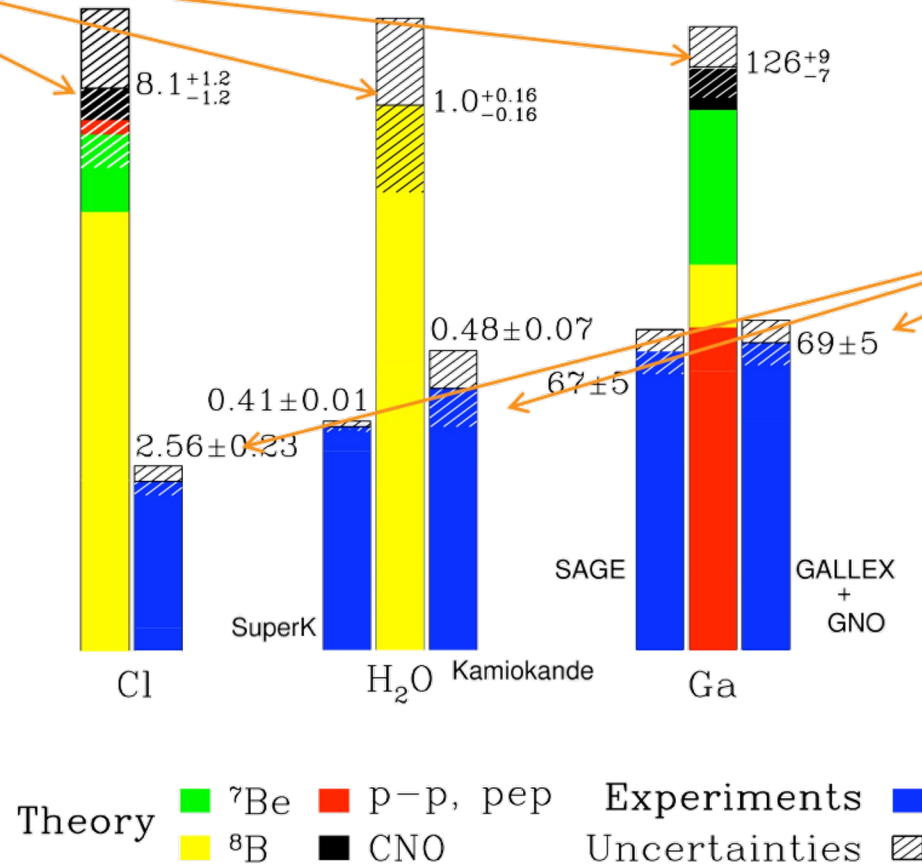


1969-
1991

Theory

Total Rates: Standard Model vs. Experiment
Bahcall-Serenelli 2005 [BS05(OP)]

Experiments

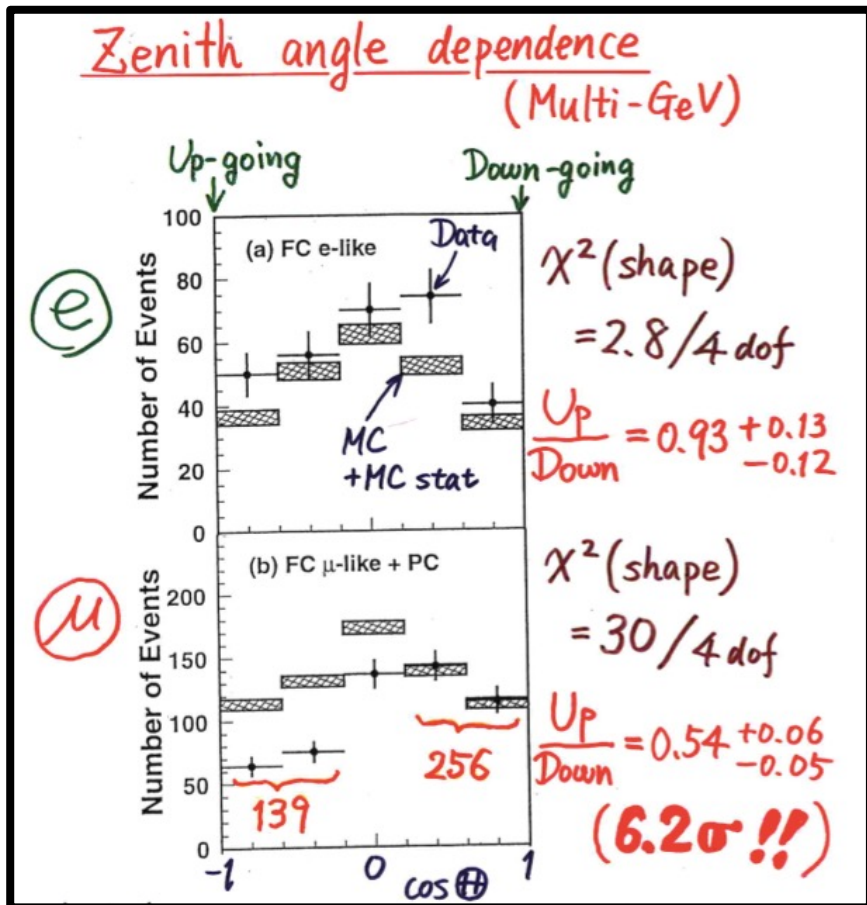
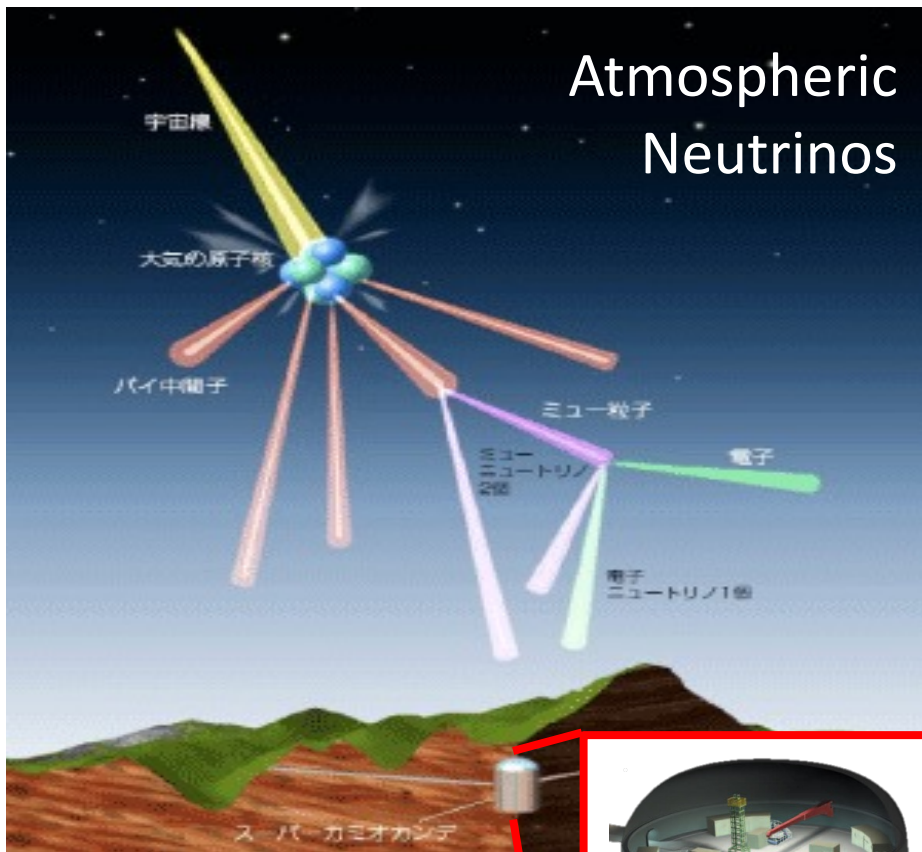


The Solution: Neutrino Oscillations

1998

Discovered in 1998 by
Super-Kamiokande

Atmospheric
Neutrinos



T. Kajita
Neutrino 1998



Neutrino Oscillations

- Create in one flavor (ν_μ), but detect in another (ν_e)



Neutrino Oscillations

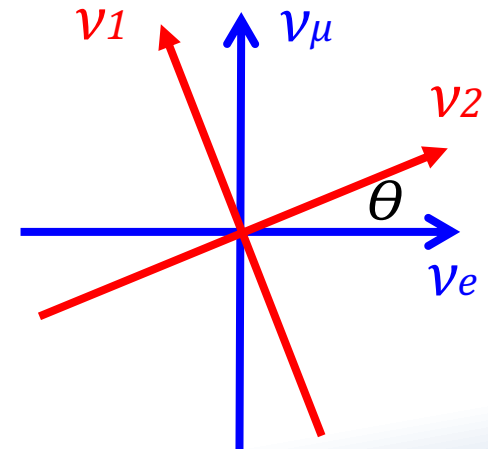
- Create in one flavor (ν_μ), but detect in another (ν_e)



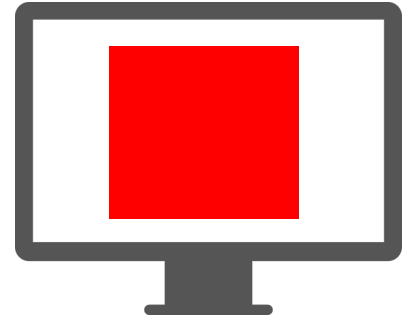
- Each flavor (e, μ) is a superposition of different masses (1, 2)

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

“Mixing Matrix”



A Colorful Analogy

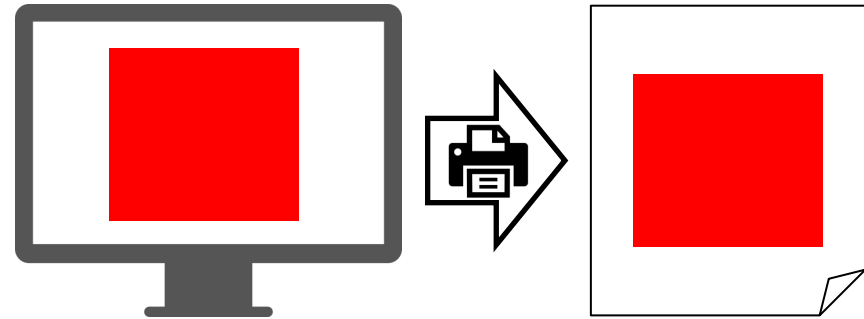


Red 100%

Green 0%

Blue 0%

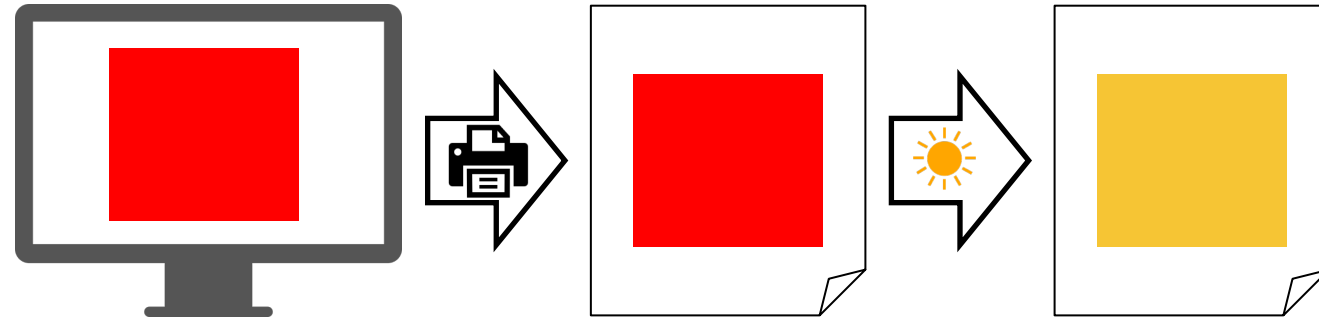
A Colorful Analogy



Red	100%
Green	0%
Blue	0%

Cyan	0%
Magenta	84%
Yellow	94%
Black	1%

A Colorful Analogy

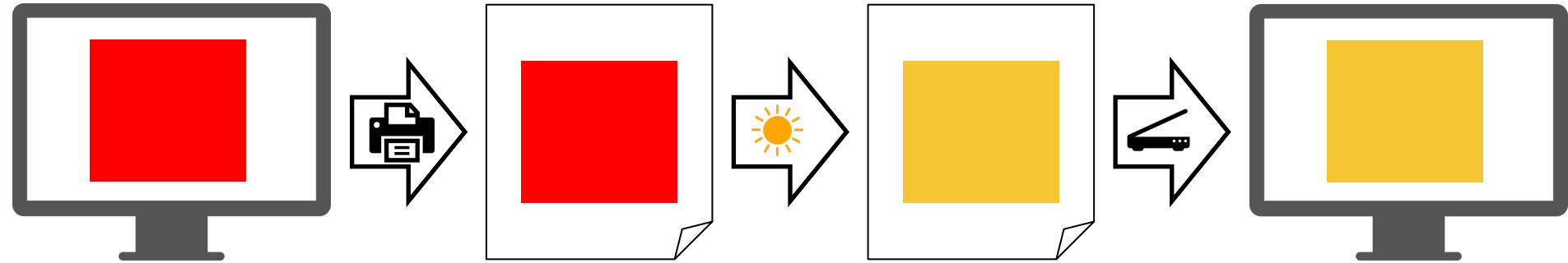


Red	100%
Green	0%
Blue	0%

Cyan	0%
Magenta	84%
Yellow	94%
Black	1%

Cyan	0%
Magenta	20%
Yellow	94%
Black	1%

A Colorful Analogy



Red 100%
Green 0%
Blue 0%

Cyan 0%
Magenta 84%
Yellow 94%
Black 1%

Cyan 0%
Magenta 20%
Yellow 94%
Black 1%

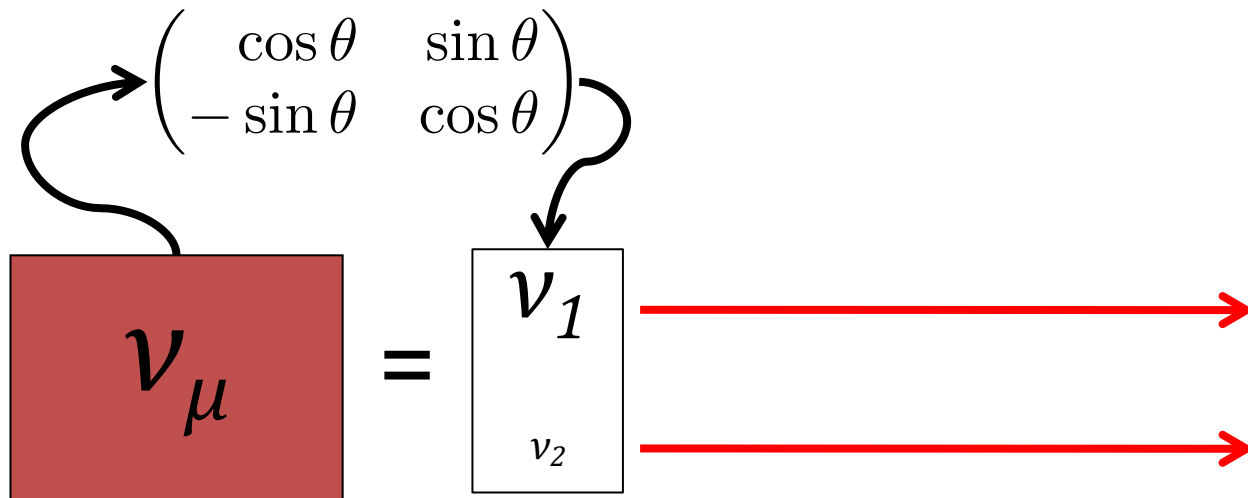
Red 50%
Green 40%
Blue 10%

Neutrino Oscillations

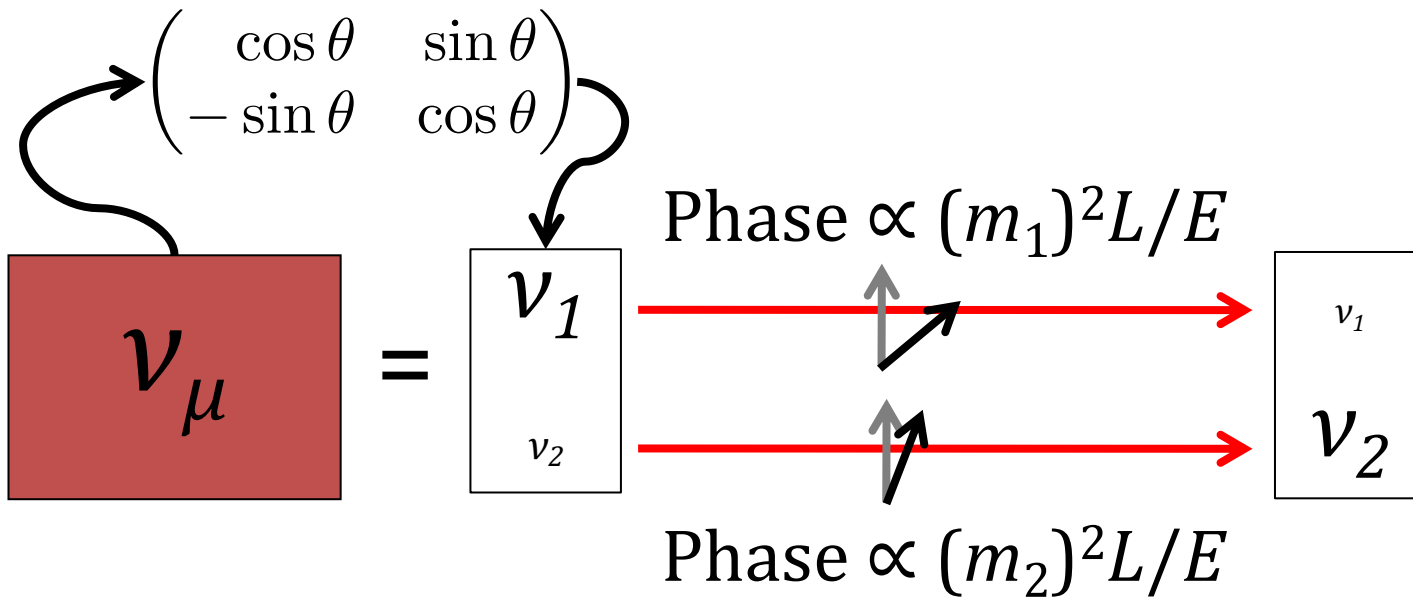


ν_{μ}

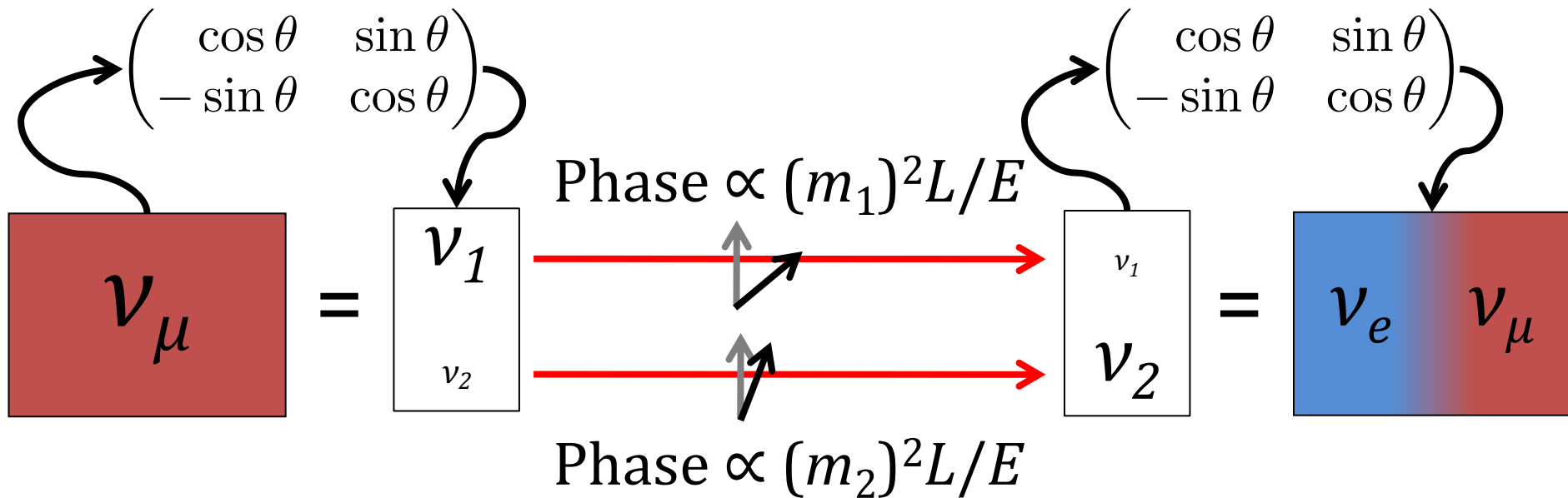
Neutrino Oscillations



Neutrino Oscillations

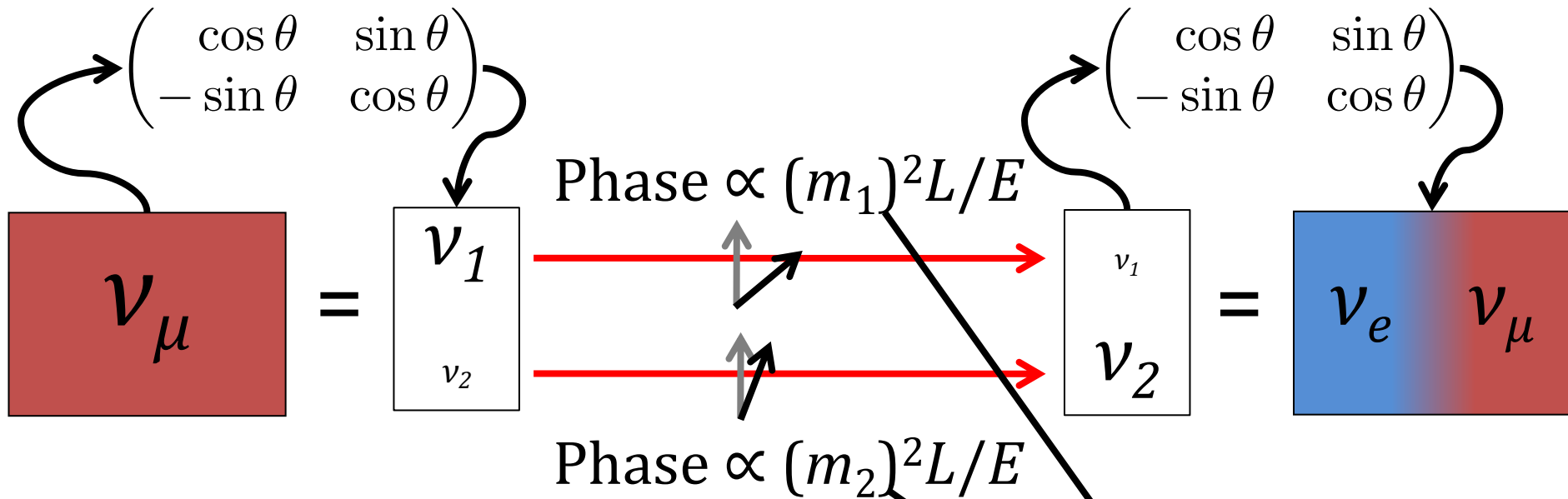


Neutrino Oscillations



Neutrino oscillations
require that neutrinos
have mass!

Neutrino Oscillations



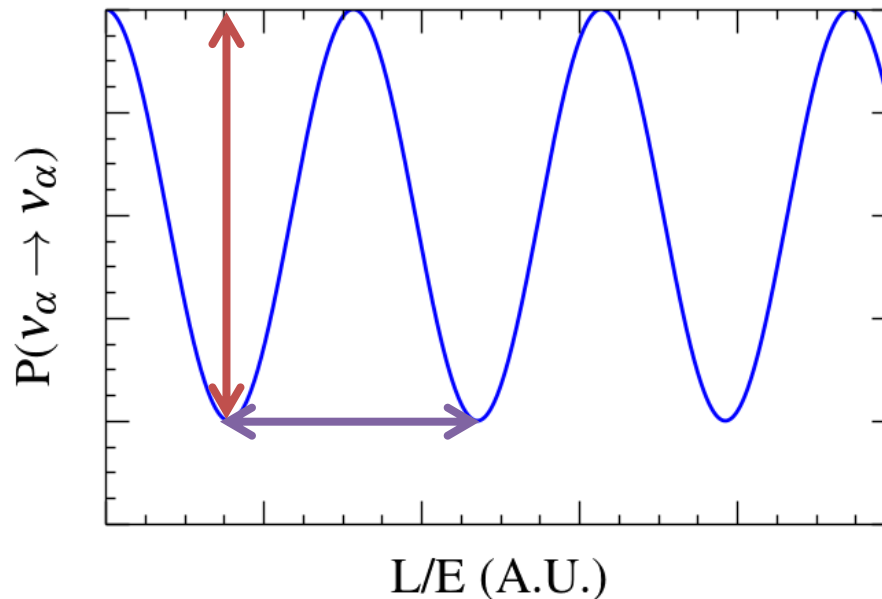
Muon Neutrino Survival Probability

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

Neutrino Oscillations

- With only 2 neutrinos, the oscillation formula is simple:

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

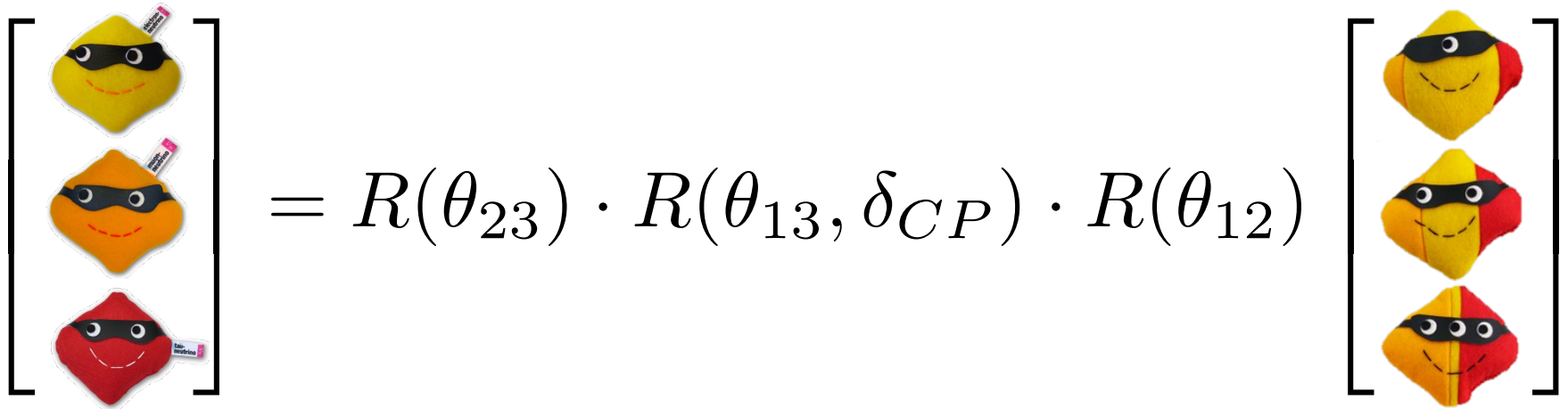


Three-flavor Neutrino Oscillations

$$\begin{matrix} e \\ \mu \\ \tau \end{matrix} \begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = U_{\text{PMNS}} \begin{bmatrix} \text{Yellow} \\ \text{Yellow/Red} \\ \text{Yellow/Red} \end{bmatrix} \begin{matrix} 1 \\ 2 \\ 3 \end{matrix}$$

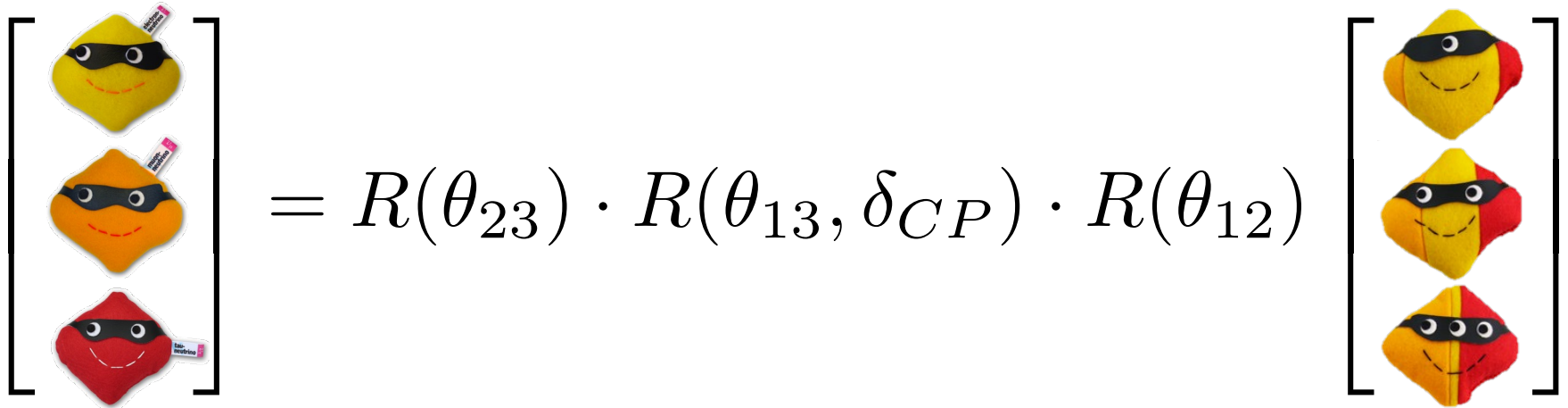
- Oscillations among the three neutrino flavors depend on:
 - The mixing matrix

Three-flavor Neutrino Oscillations

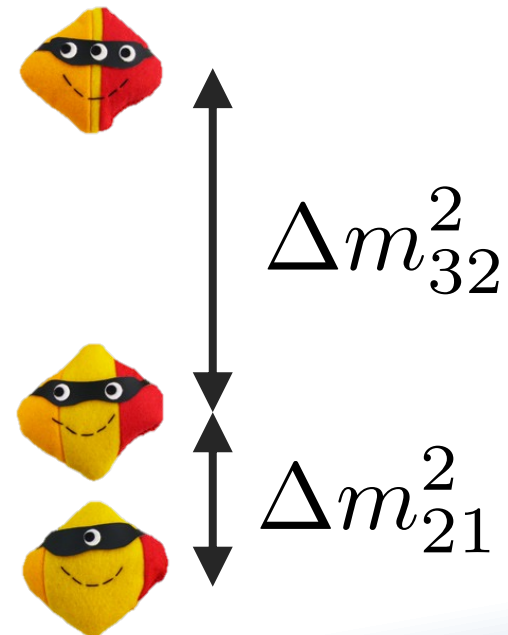

$$\begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix}$$

- Oscillations among the three neutrino flavors depend on:
 - The mixing matrix
 - $\theta_{23}, \theta_{13}, \delta_{CP}, \theta_{12}$

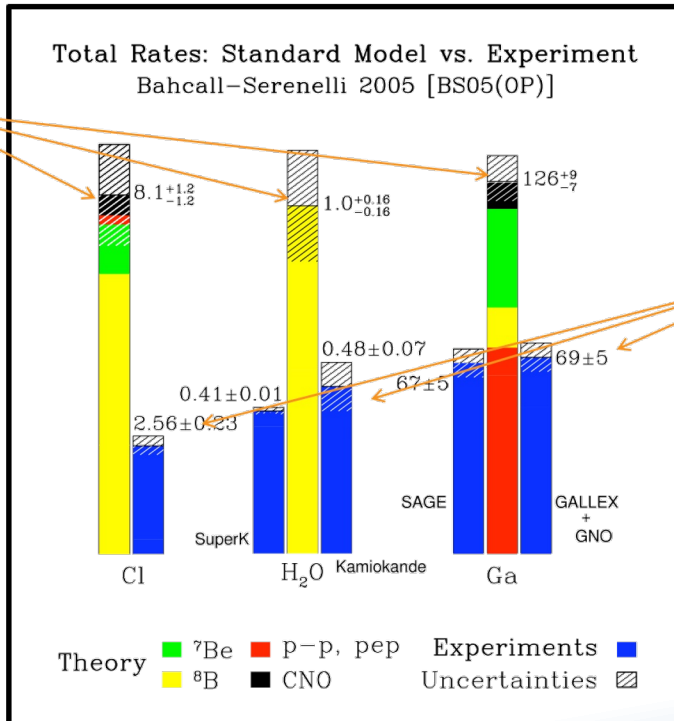
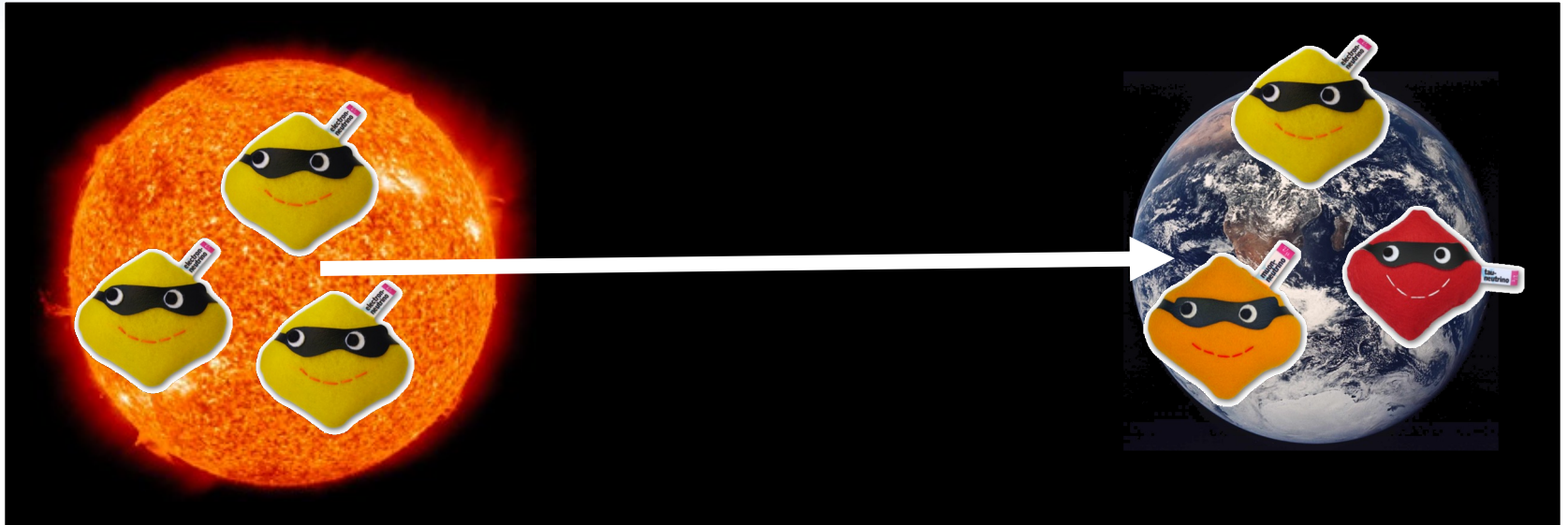
Three-flavor Neutrino Oscillations


$$\begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix}$$

- Oscillations among the three neutrino flavors depend on:
 - The mixing matrix
 - $\theta_{23}, \theta_{13}, \delta_{CP}, \theta_{12}$
 - The mass differences
 - $\Delta m^2_{32}, \Delta m^2_{21}$

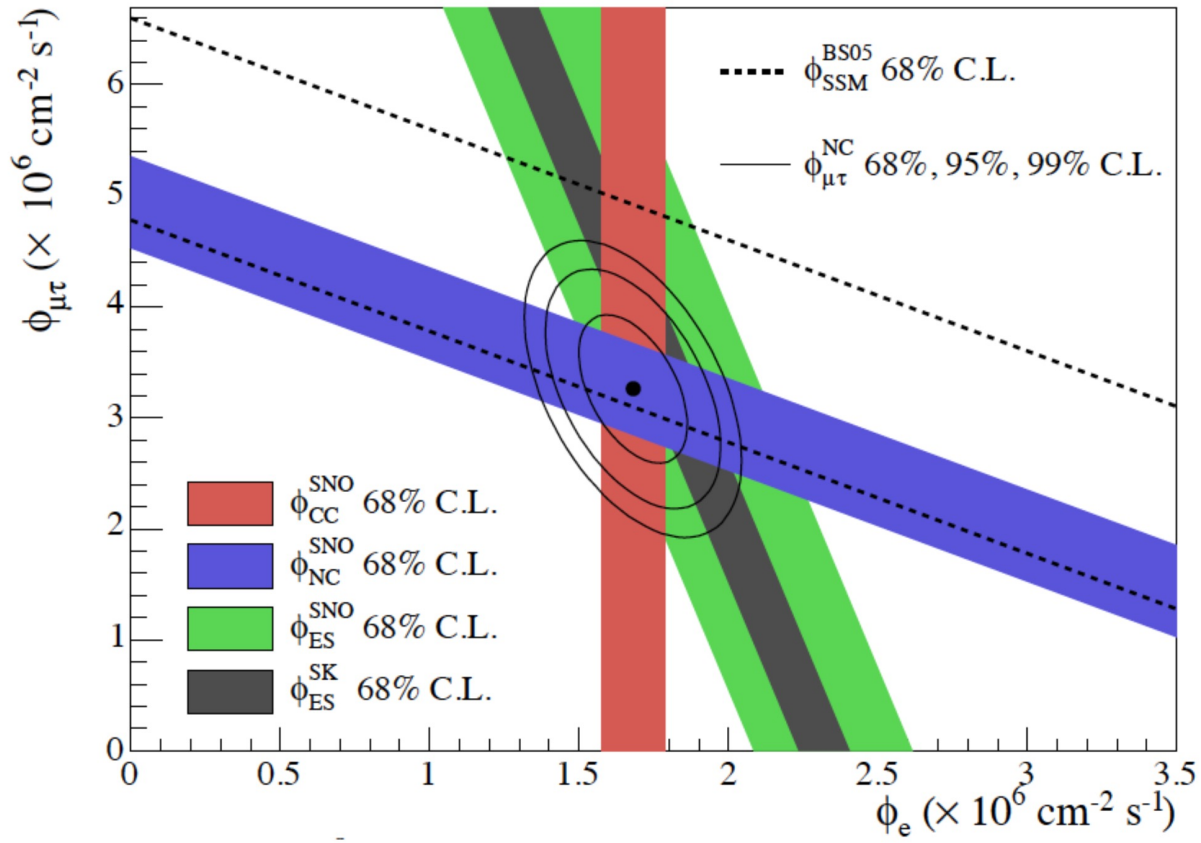


Solar Neutrinos

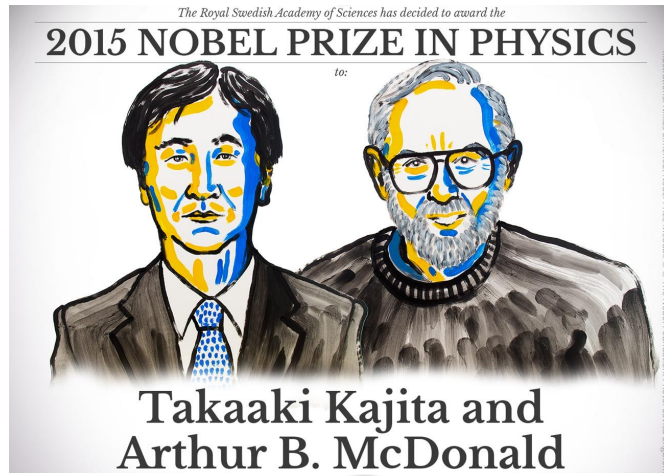


Experiments

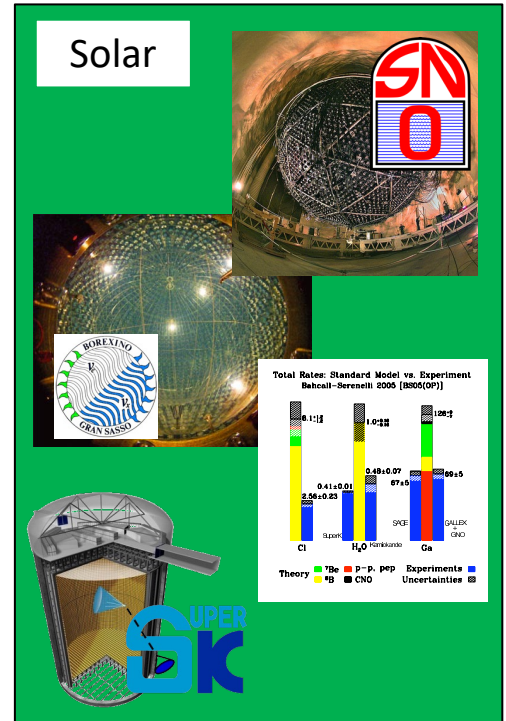




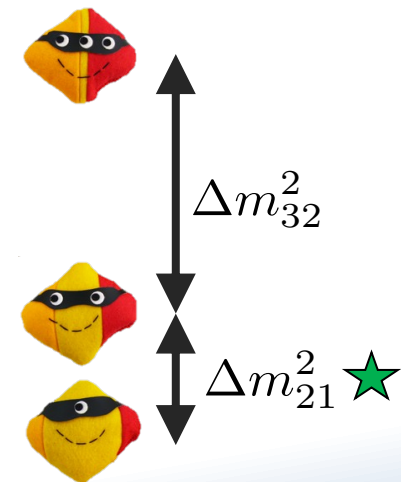
- The definitive solution came from the SNO experiment, which measured both the ν_e and all- ν fluxes together.



Understanding oscillations: a world-wide effort



$$\begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix}$$



Understanding oscillations: a world-wide effort

Reactor

DOUBLE
Daya Bay 13
IRENO θ_{13}

Reactor

KamLAND
JUNO

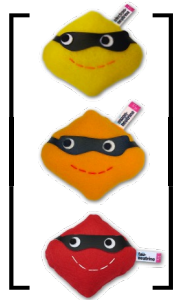
Solar

SNOLAB
BOREXINO
GALLEX
GNO

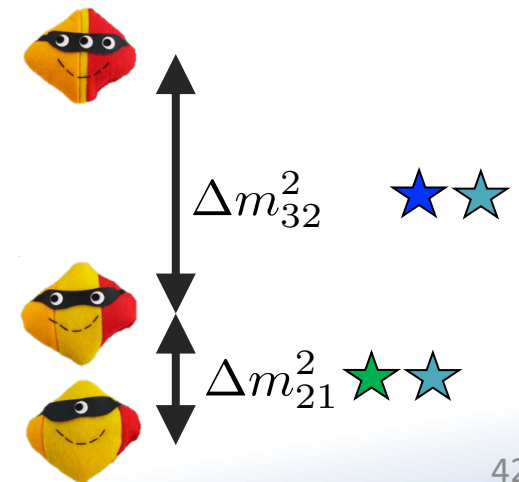
Total Rate: Standard Model vs. Experiment
Bahcall-Serenelli 2005 [B800(OP)]

Element	Standard Model	Experiment
Cl	4.1 ± 1.1	3.56 ± 0.23
H ₂ O	1.0 ± 0.2	0.41 ± 0.01
Ar	1.0 ± 0.2	0.49 ± 0.07
Ge	1.0 ± 0.2	0.74 ± 0.05
Ga	1.0 ± 0.2	0.69 ± 0.05

Theory: θ_{13} (green), θ_{12} (red), θ_{23} (blue), δ_{CP} (purple), θ_{13} (yellow), CNO (orange), Experiments (grey), Uncertainties (white)



$$= R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$$



Understanding oscillations: a world-wide effort

Accelerator and Atmospheric

MINOS, NOVA, OPERA, T2K

DUNE DEEP UNDERGROUND NEUTRINO EXPERIMENT

ICECUBE SOUTH POLE NEUTRINO OBSERVATORY

Solar

SN, BOREXINO, SUPER-K

Total Rate: Standard Model vs. Experiment Bahcall-Serenelli 2005 (BSP)

Flavor	Theory	Experiment
Cl	0.1 ± 0.1	0.41 ± 0.01
Ar	0.00 ± 0.00	0.56 ± 0.03
H ₂ O	0.00 ± 0.00	0.48 ± 0.07
SK1	0.00 ± 0.00	0.74 ± 0.05
SK2	0.00 ± 0.00	0.80 ± 0.05
SK3	0.00 ± 0.00	0.80 ± 0.05

Legend: Theory (green), Exp. (red), P-P, PEP (blue), CNO (yellow), Experiments (orange), Uncertainties (grey)

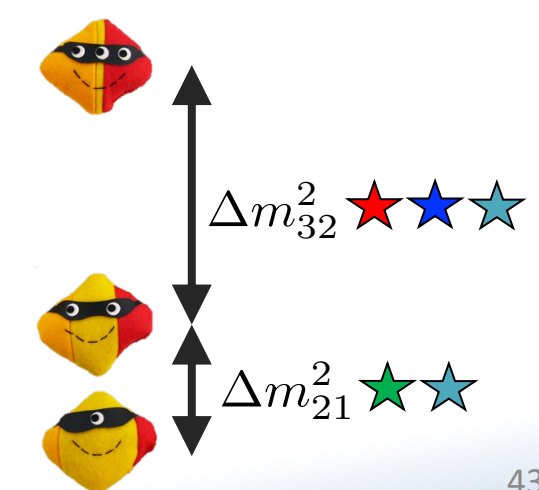
Reactor

DOUBLE CHOOZ, Daya Bay 13, IRENO

Reactor

KamLAND, JUNO

$$\begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix}$$



Understanding oscillations: a world-wide effort

Accelerator and Atmospheric

MINOS, NOVA, OPERA, DUNE DEEP UNDERGROUND NEUTRINO EXPERIMENT, ICECUBE SOUTH POLE NEUTRINO OBSERVATORY, T2K

Solar

SNOLAB, BOREANO, GALLEX, GNO

Total Rate: Standard Model vs. Experiment
Bahcall-Serenelli 2005 [ISS05(OP)]

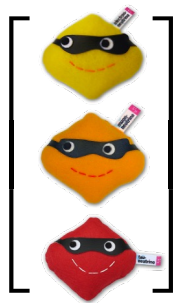
Flavor	Theory	Experiments
Cl	0.11	2.56 ± 0.23
Ar	0.41 ± 0.01	0.48 ± 0.07
H ₂ O	1.0 ± 0.1	0.74 ± 0.07
SK	0.48 ± 0.07	0.69 ± 0.05

Reactor

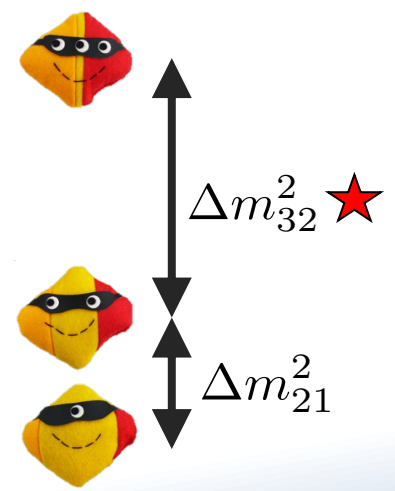
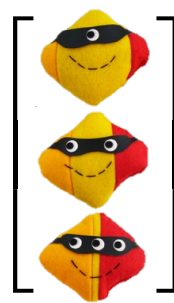
DOUBLE CHOOZ, Daya Bay 13, IRENO

Reactor

KamLAND, JUNO



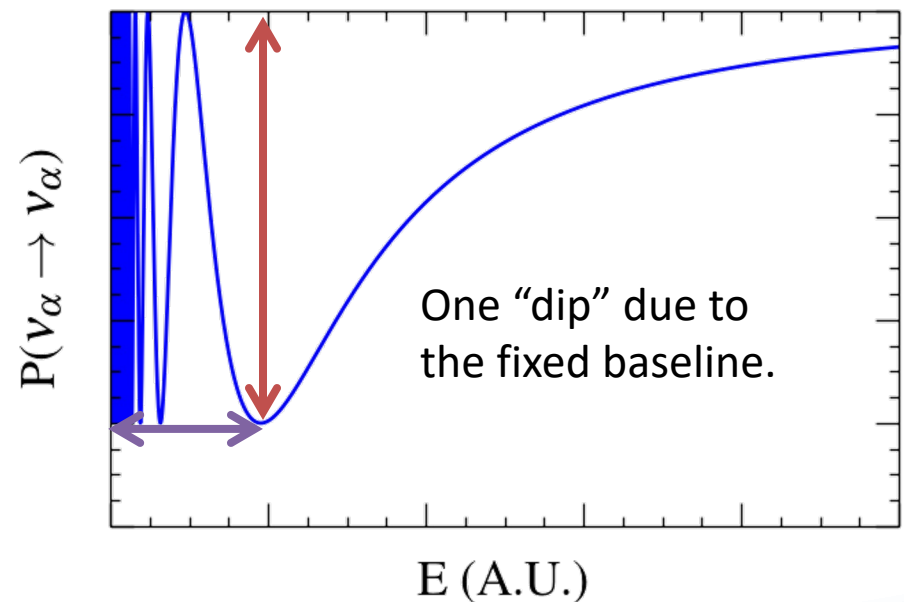
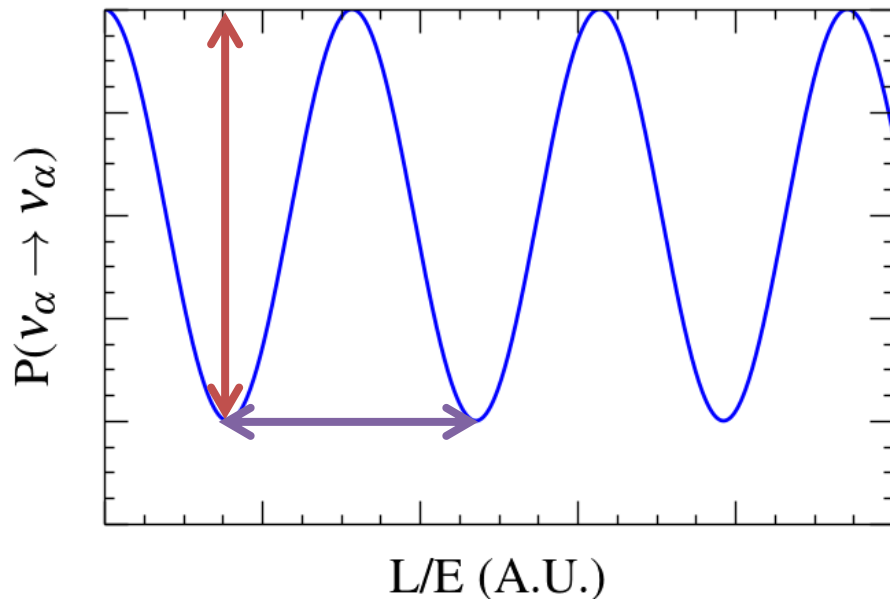
$$= \star R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$$



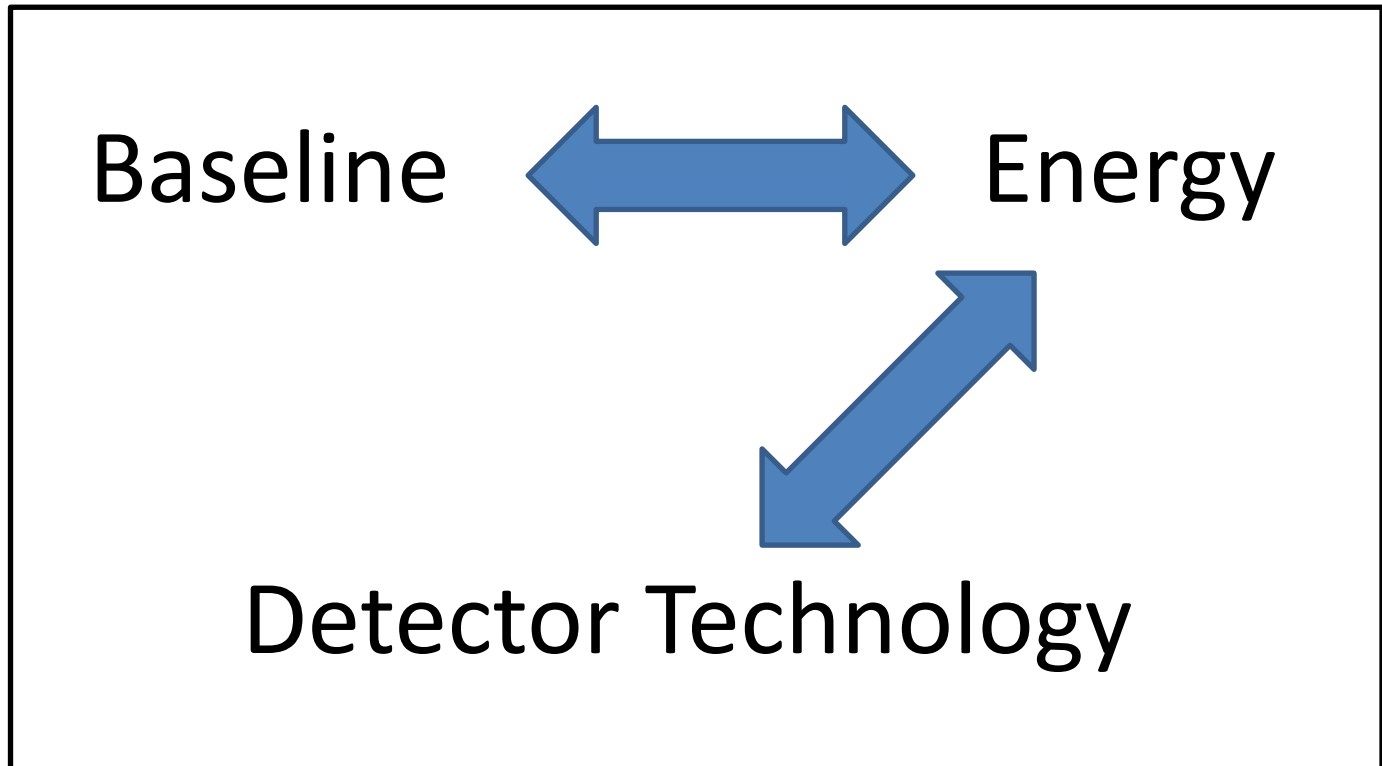
How to study oscillations: Disappearance

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - \left(\sin^2(2\theta_{13}) \sin^2(\theta_{23}) + \cos^4(\theta_{13}) \sin^2(2\theta_{23}) \right) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$$

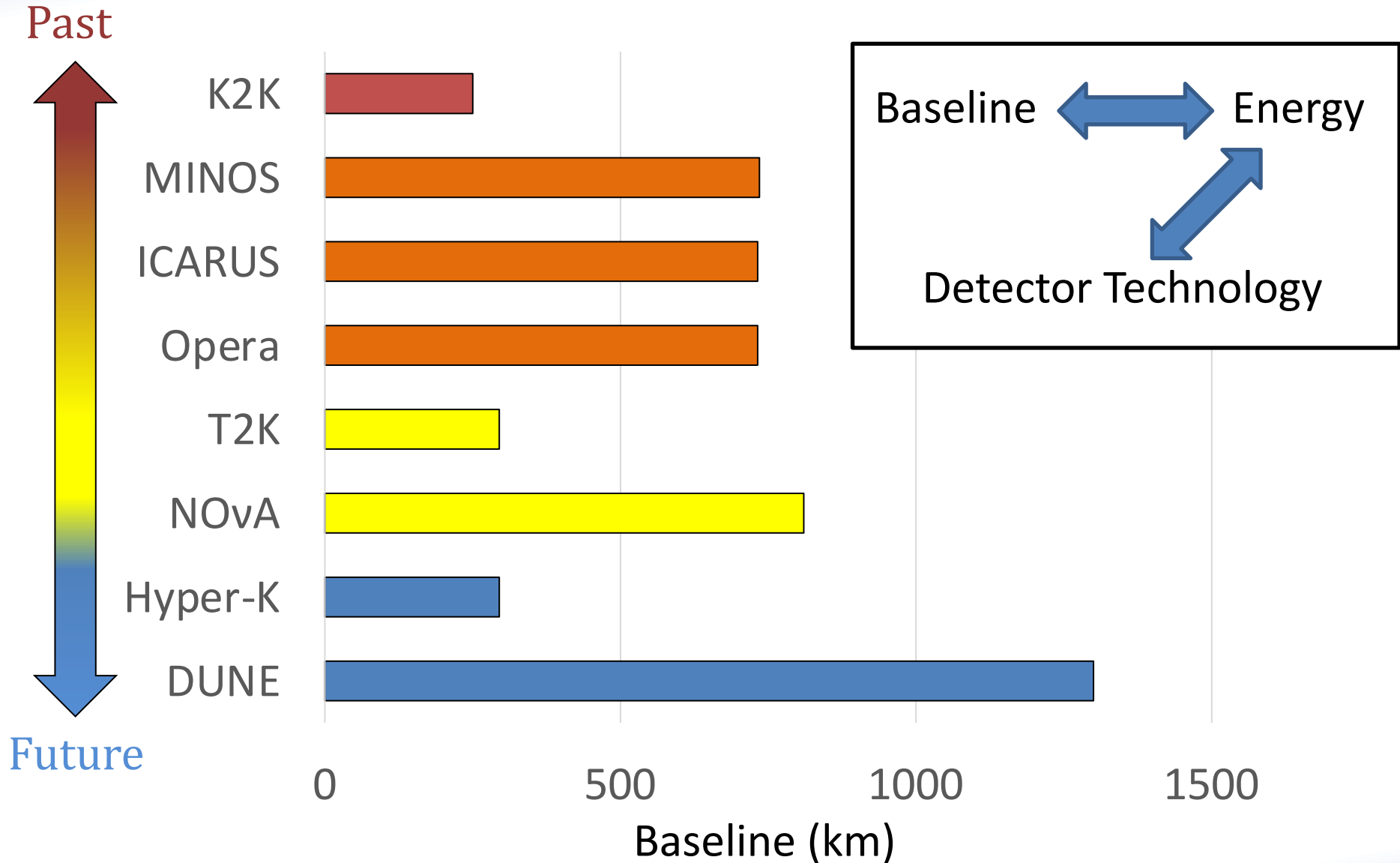
Sub-dominant term due to small θ_{13}



Designing an Accelerator ν Experiment

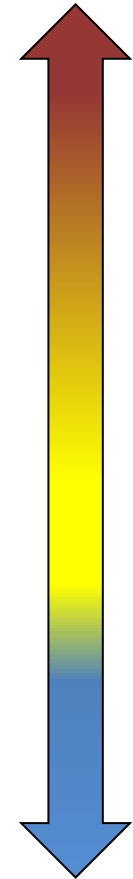


Designing an Accelerator ν Experiment

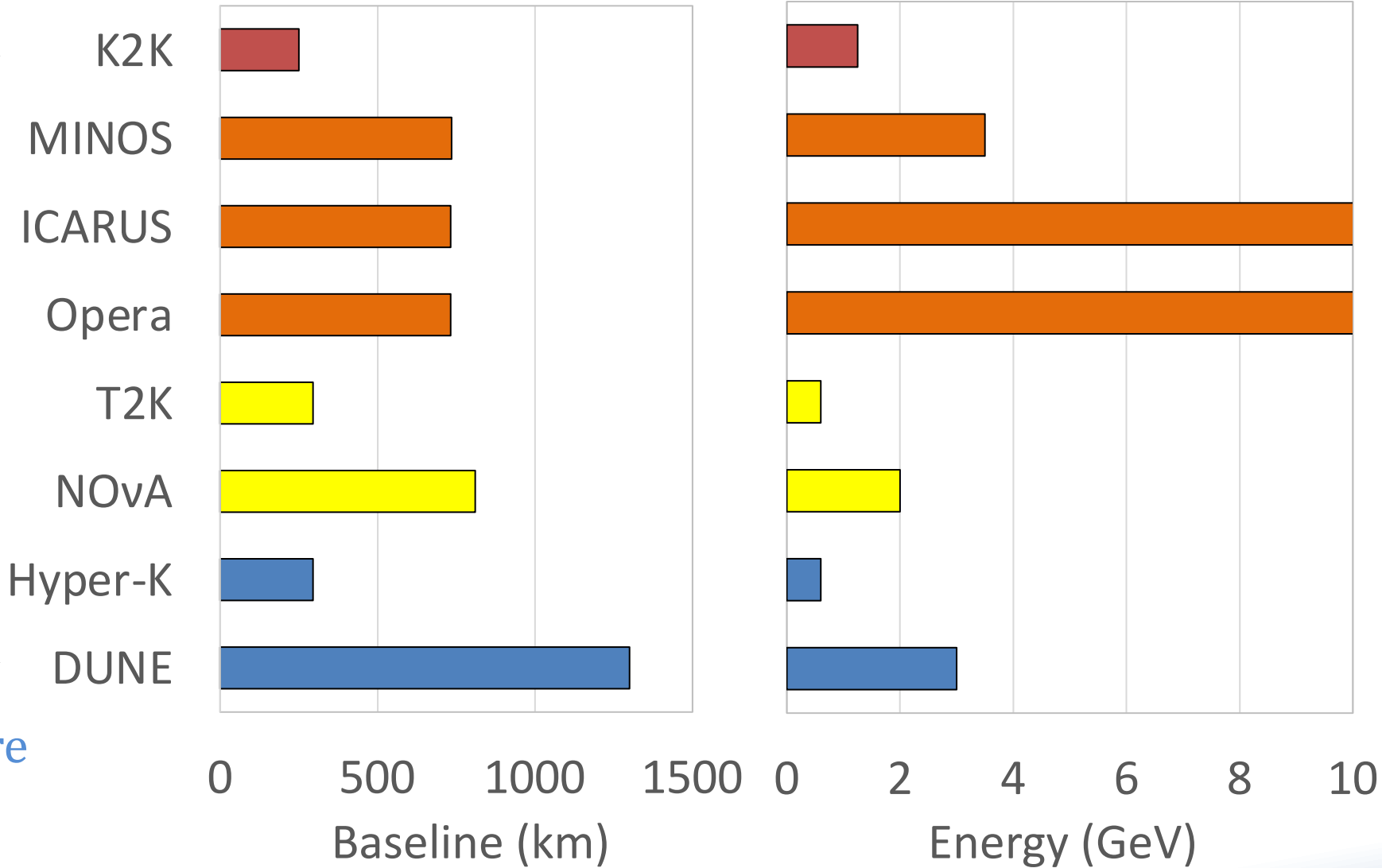


Designing an Accelerator ν Experiment

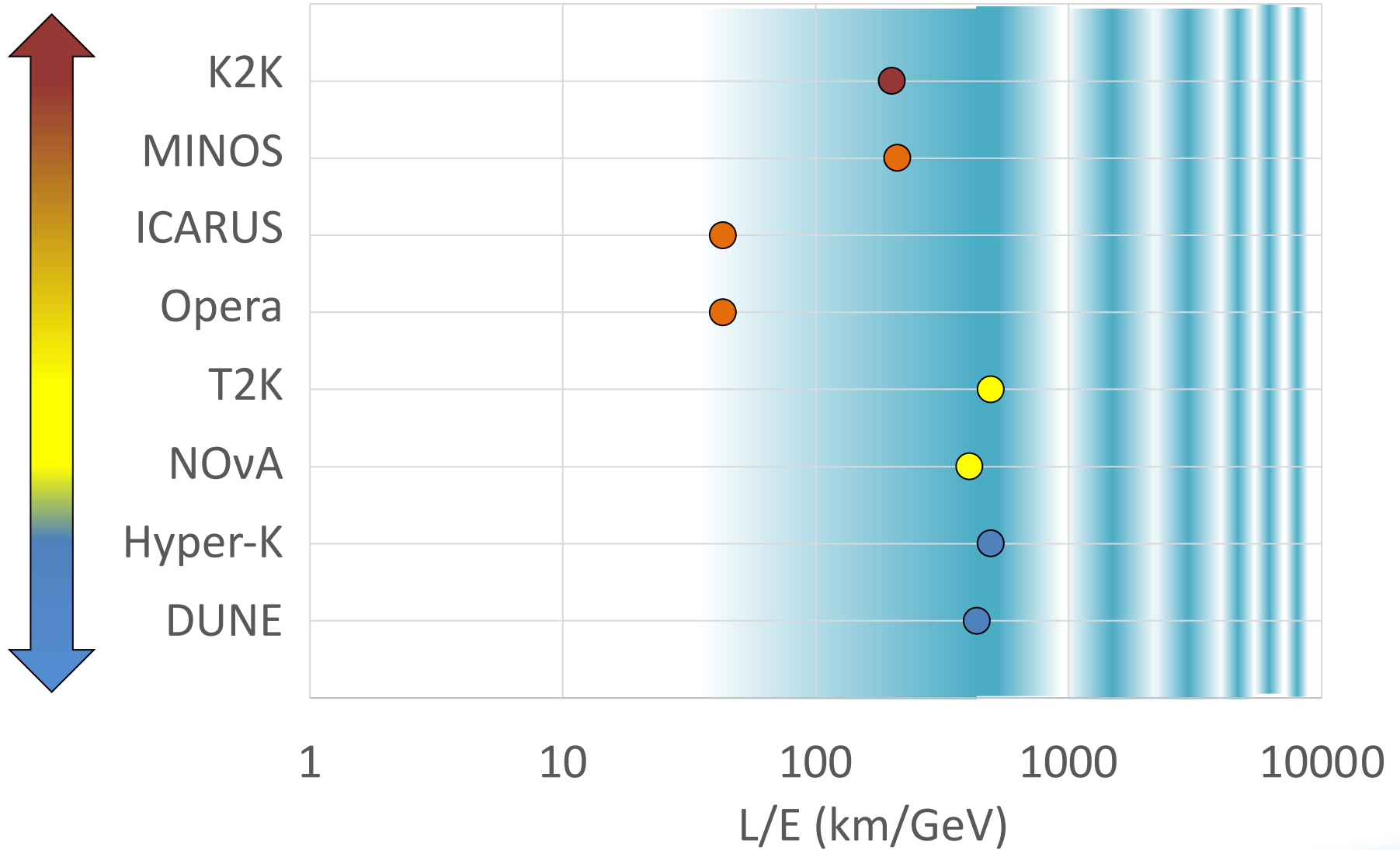
Past



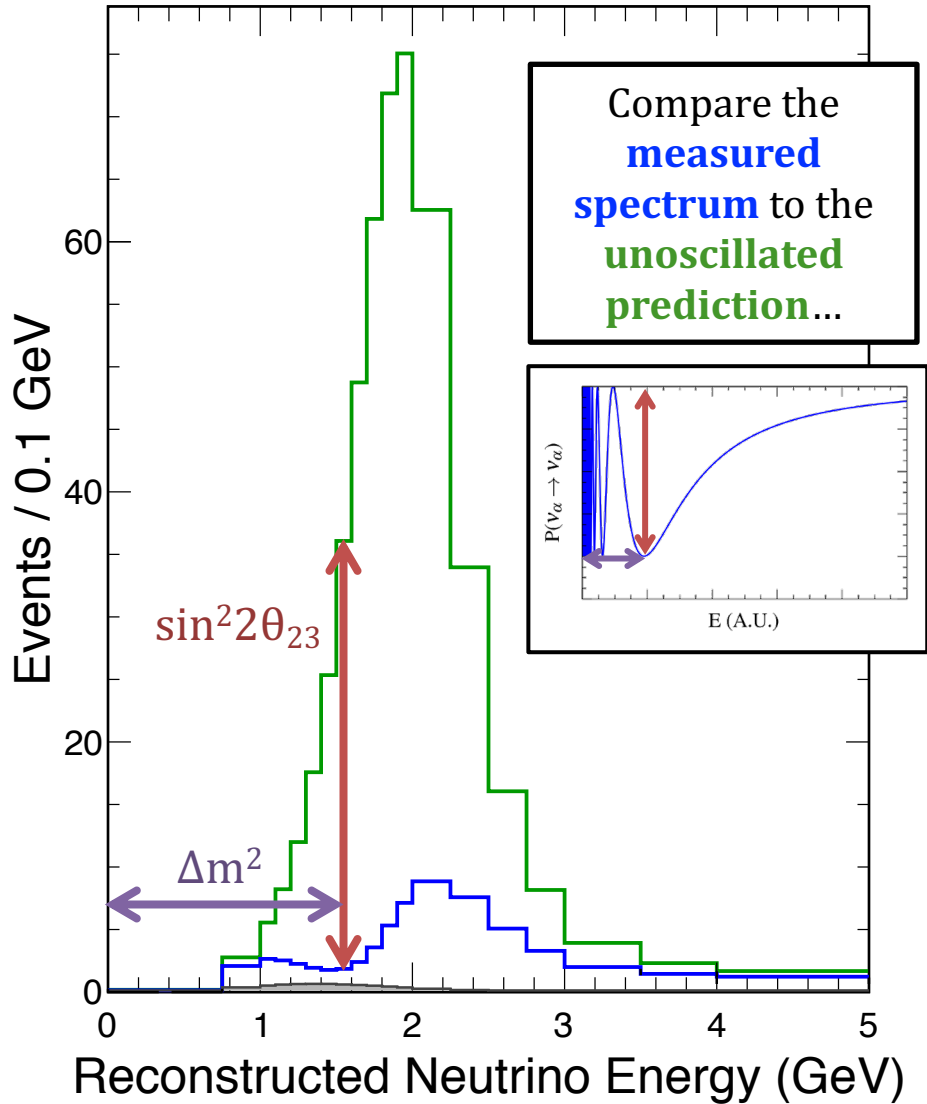
Future



Designing an Accelerator ν Experiment

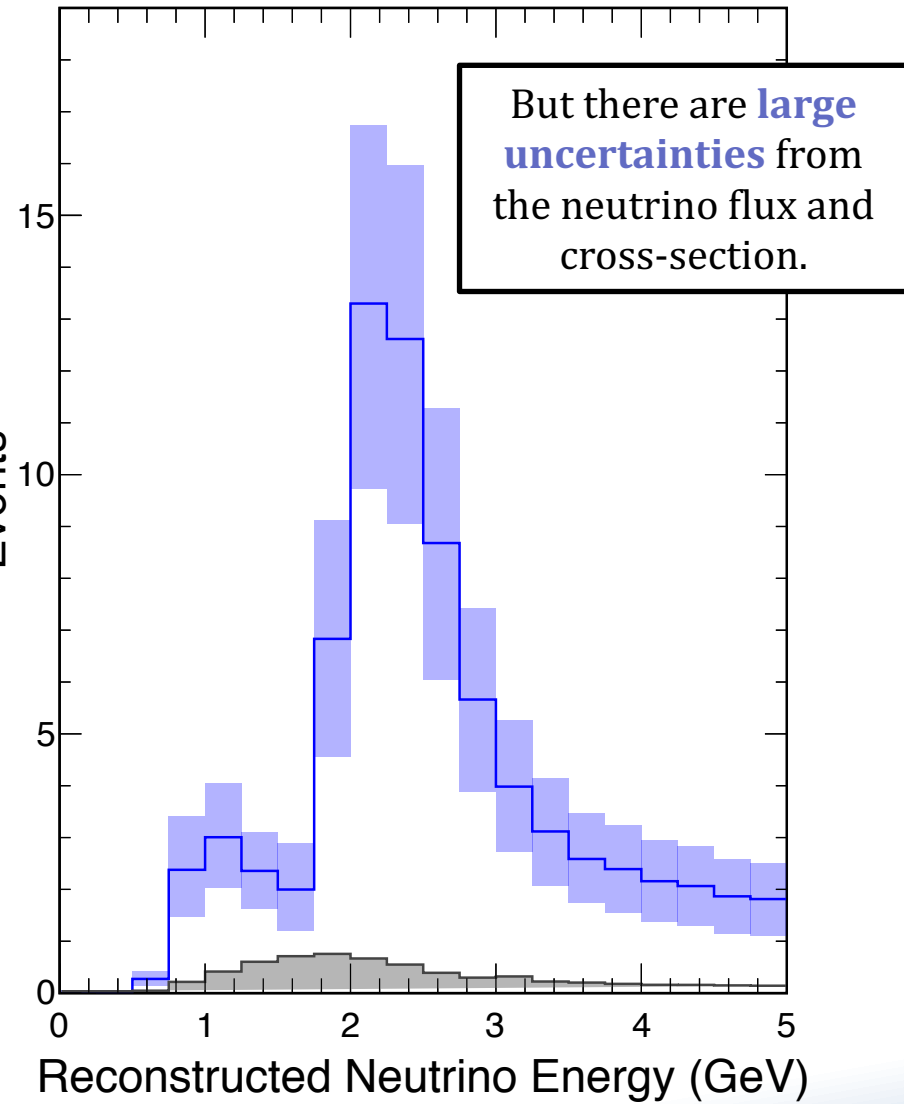
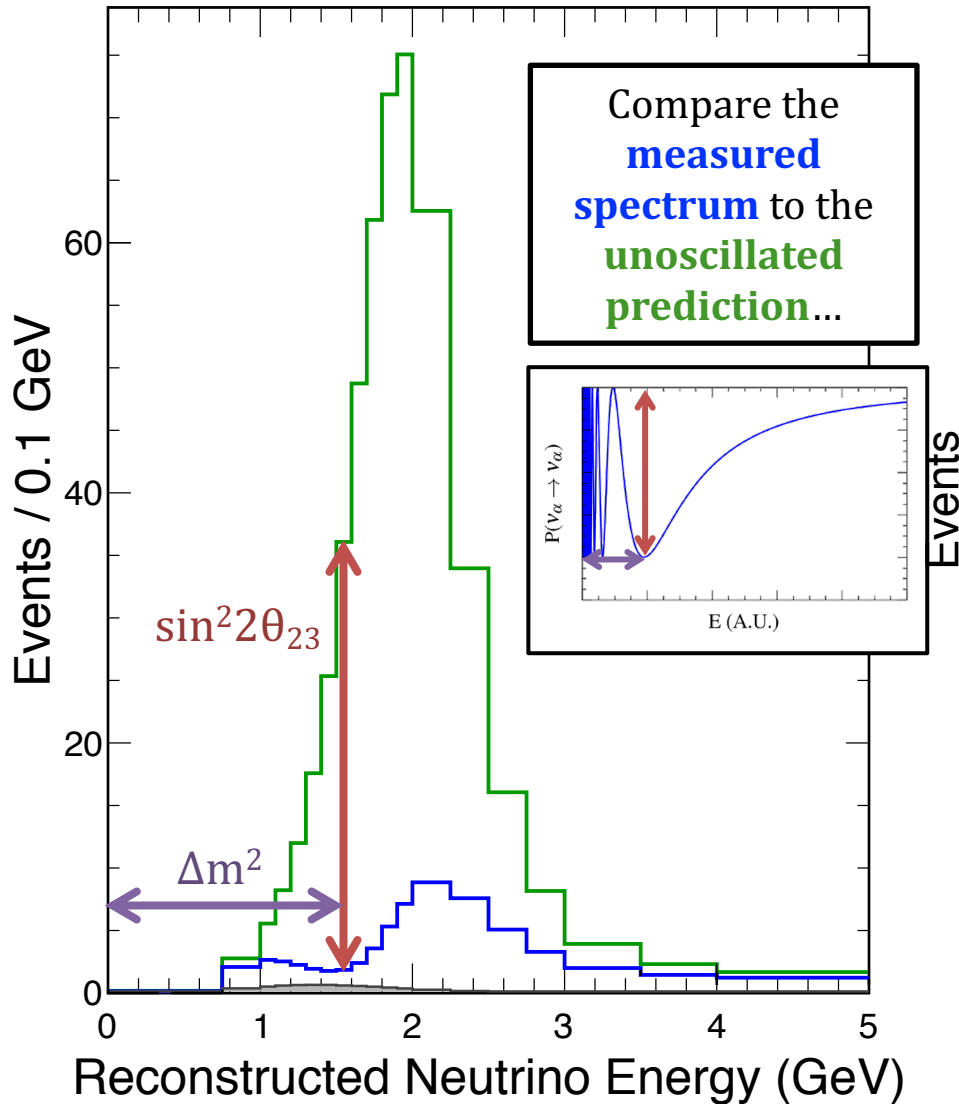


How to study oscillations: Disappearance



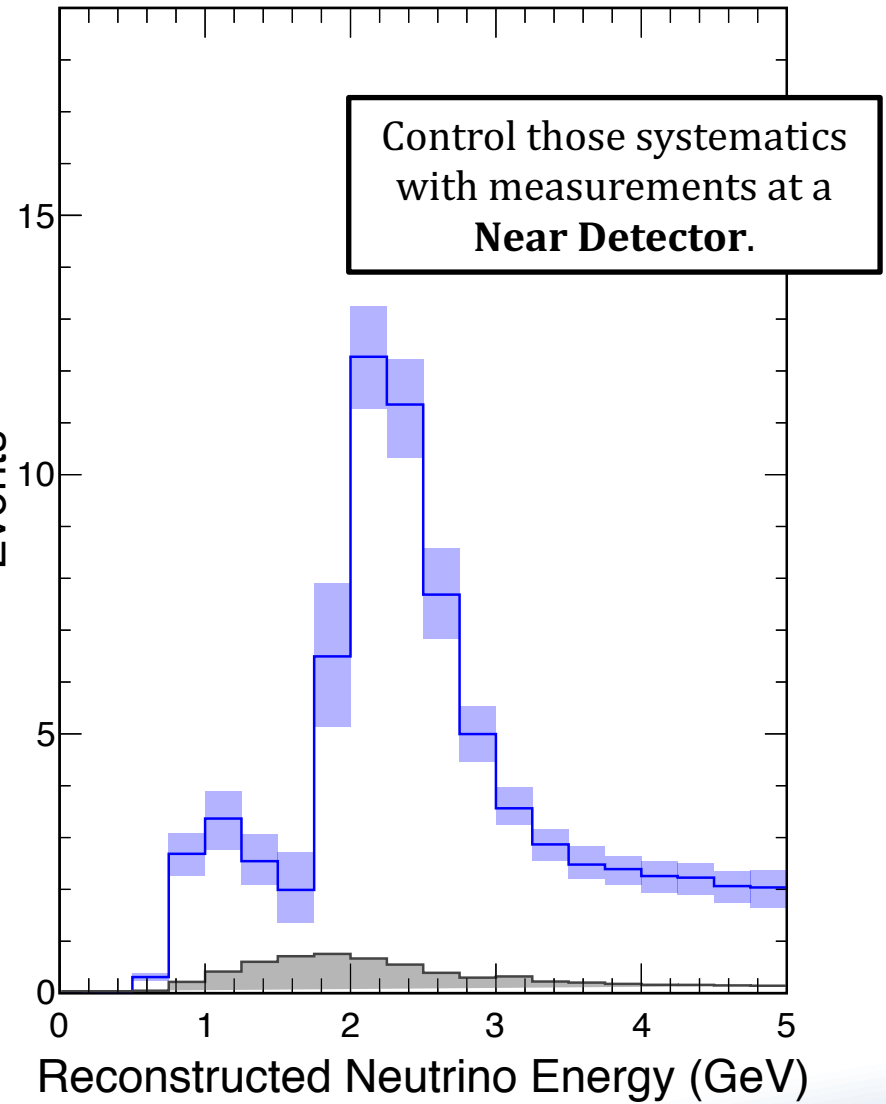
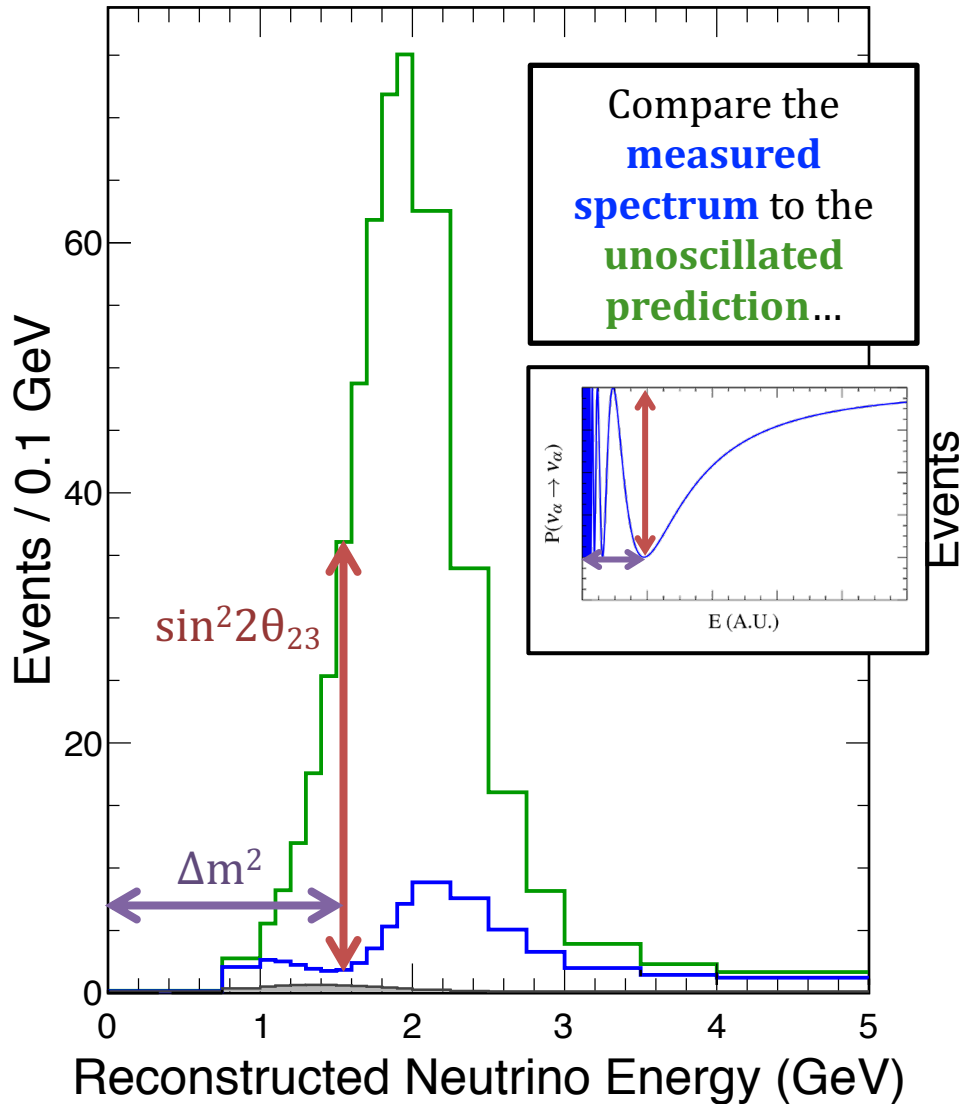
How to study oscillations: Disappearance

NOvA Simulation



How to study oscillations: Disappearance

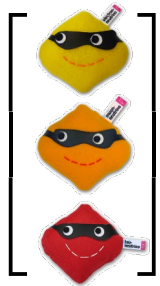
NOvA Simulation



How to study oscillations: Appearance

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &\approx \left| \sqrt{P_{\text{atm}}} e^{-i(\Delta_{32} + \delta_{CP})} + \sqrt{P_{\text{sol}}} \right|^2 \\
 &\approx P_{\text{atm}} + P_{\text{sol}} + 2\sqrt{P_{\text{atm}}P_{\text{sol}}} (\cos \Delta_{32} \cos \delta_{CP} \mp \sin \Delta_{32} \sin \delta_{CP}) \\
 &\quad \swarrow \\
 \sqrt{P_{\text{atm}}} &= \sin(\theta_{23}) \sin(2\theta_{13}) \frac{\sin(\Delta_{31} - aL)}{\Delta_{31} - aL} \Delta_{31}
 \end{aligned}$$

- Depends some on *every* oscillation parameter.
- **Benefit:** can answer more questions.
- **Drawback:** degeneracies make things difficult.



$$= R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$$



$$\Delta m_{32}^2 \rightarrow O(10^{-3} \text{eV}^2)$$



$$\Delta m_{21}^2 \rightarrow O(10^{-5} \text{eV}^2)$$

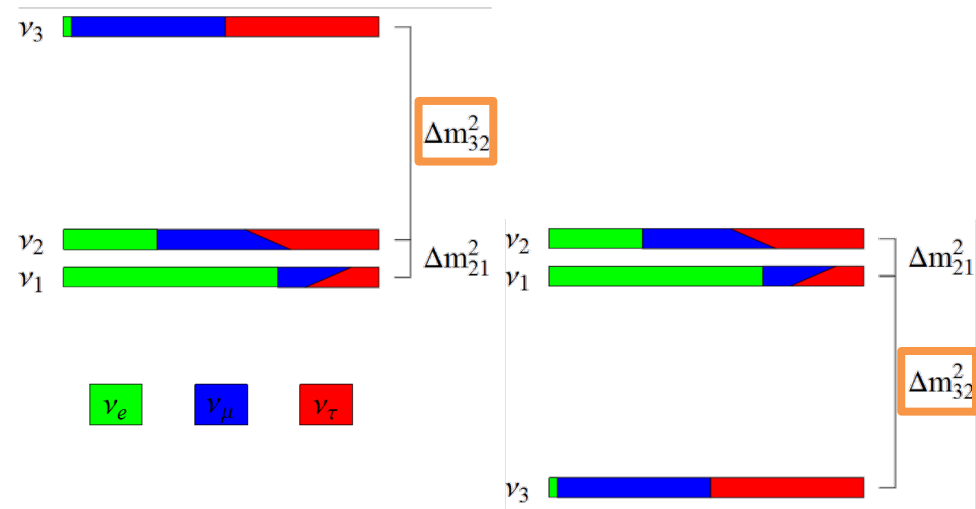


Open questions in neutrino oscillations

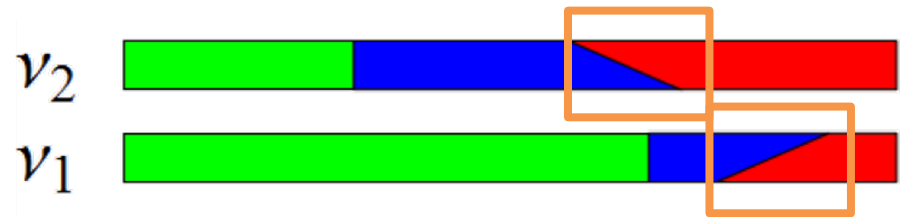
1. Do neutrino oscillations violate CP symmetry directly via δ_{CP} ?

$$R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$$

2. Is the mass hierarchy “normal” or “inverted?”



3. What is the “octant” of θ_{23} ?
 – Or is the mixing “maximal” (e.g. $\theta_{23} = 45^\circ$)?



Aside – what is CP symmetry?

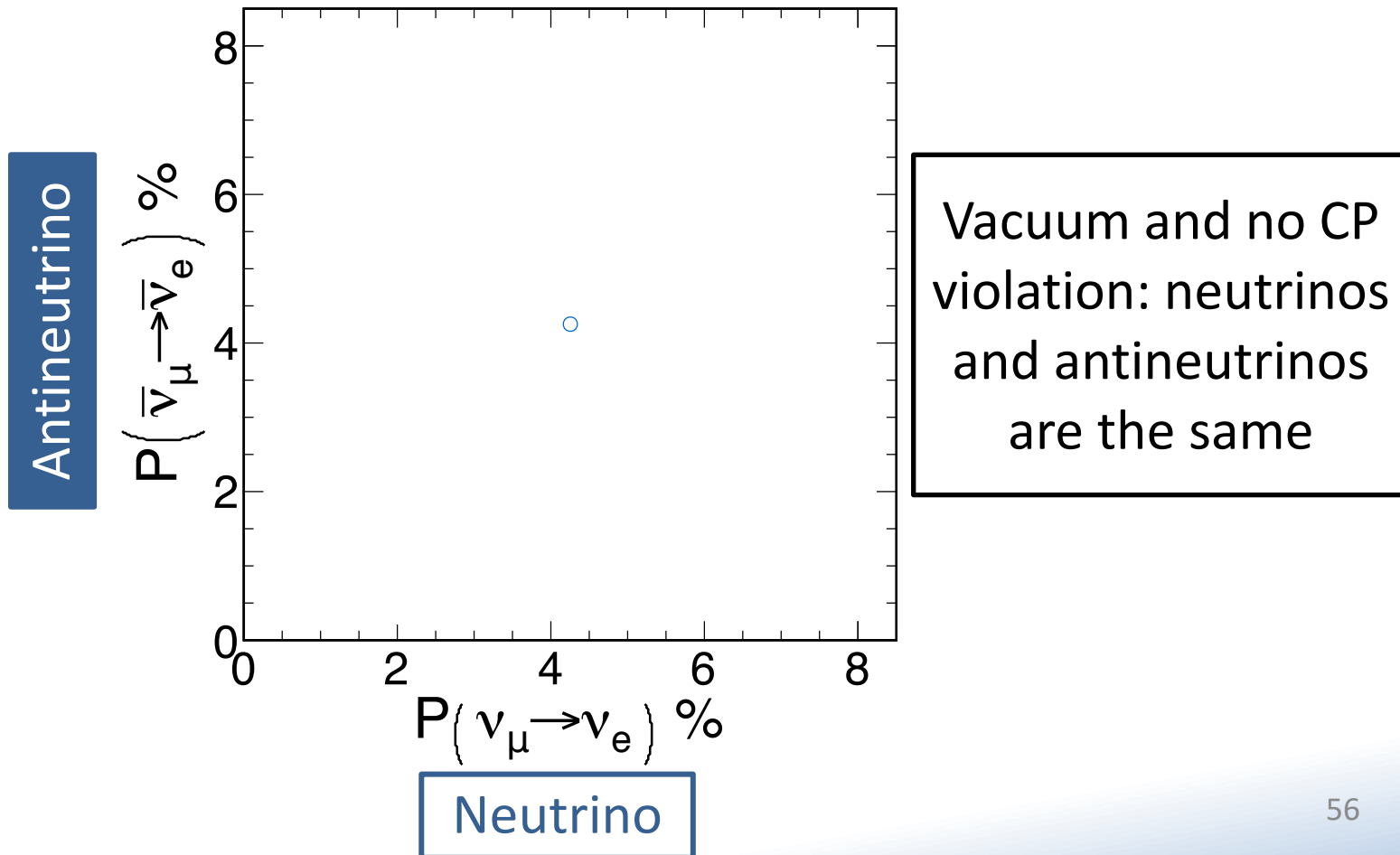
- We are very interested in symmetries and broken symmetries since they are deeply related to fundamental laws.
- **C = charge**, which means particle-antiparticle symmetry
- **P = parity**, which means symmetry under mirror reflections
- Large violations of C and P symmetry are common, but violations of C & P together are very rare.
- Important: more CP violation is needed to explain why the universe is made of matter!



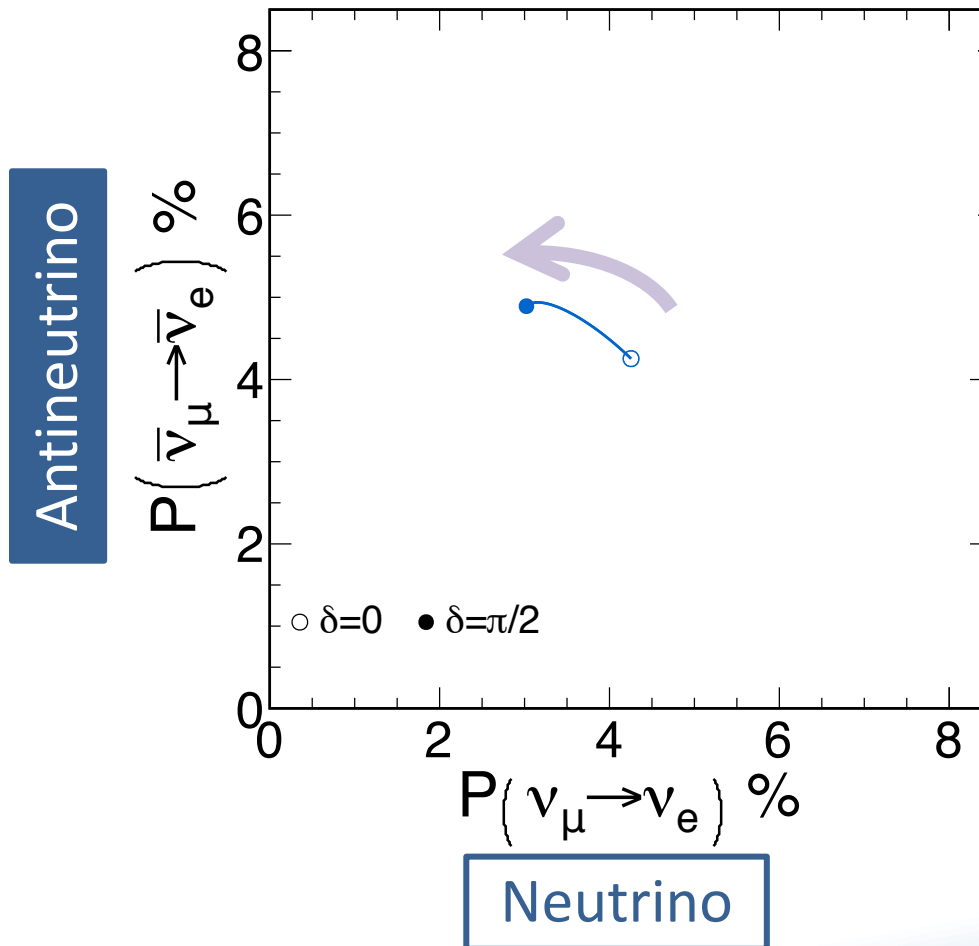
Emmy Noether



1. Is the mass hierarchy “normal” or “inverted?”
2. Do neutrino oscillations violate CP symmetry?
3. What is the “octant” of θ_{23} ?

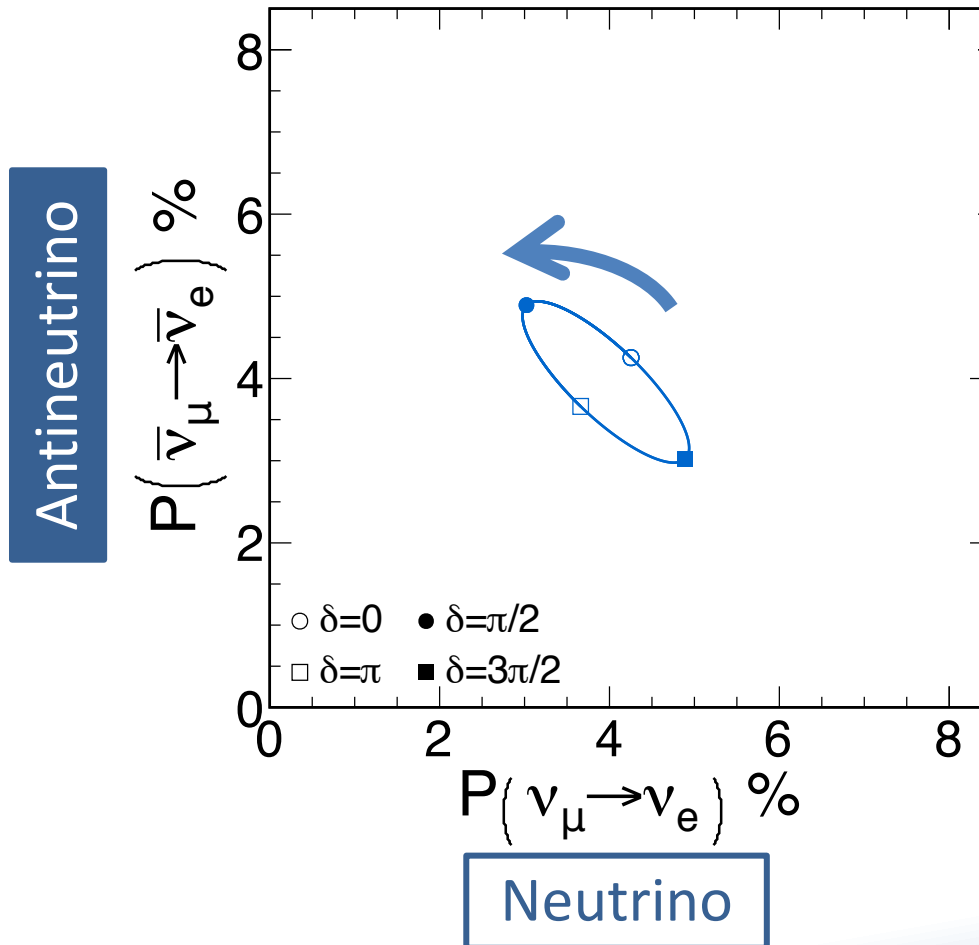


1. Is the mass hierarchy “normal” or “inverted?”
2. Do neutrino oscillations violate CP symmetry?
3. What is the “octant” of θ_{23} ?



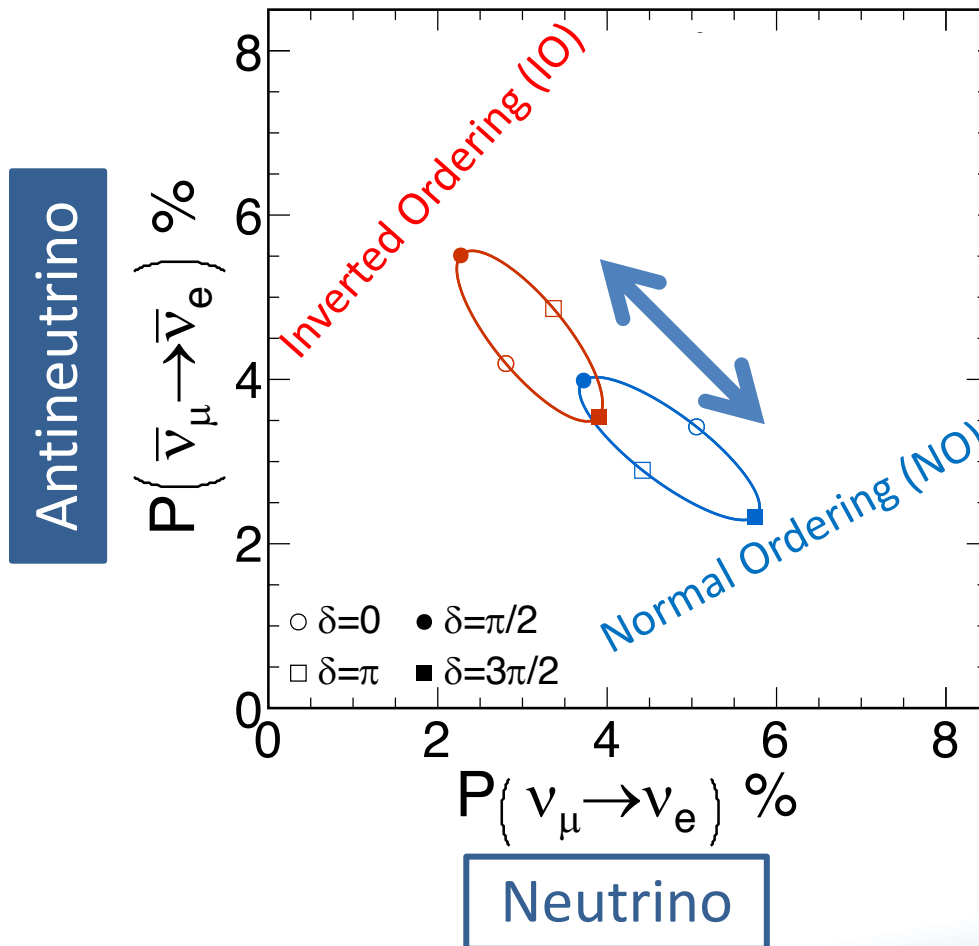
CP-violation through δ creates opposite effects in neutrinos and antineutrinos

1. Is the mass hierarchy “normal” or “inverted?”
2. Do neutrino oscillations violate CP symmetry?
3. What is the “octant” of θ_{23} ?



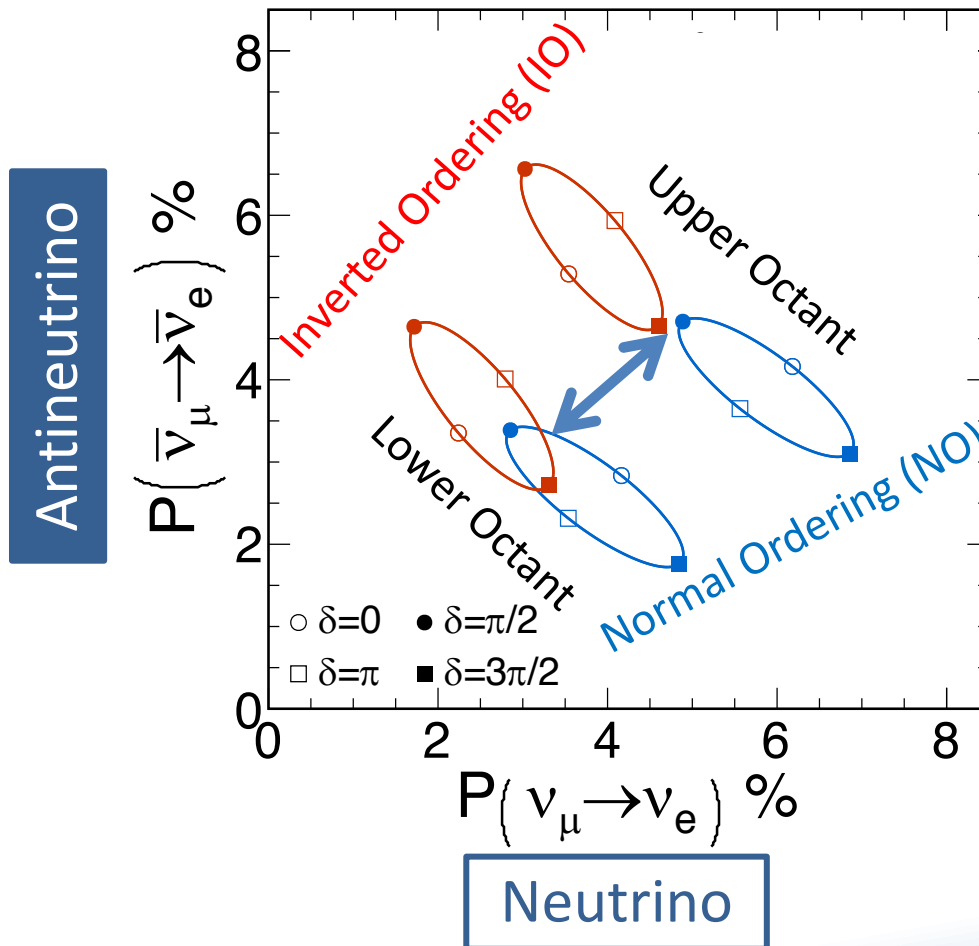
CP-violation through δ creates opposite effects in neutrinos and antineutrinos

1. Is the mass hierarchy “normal” or “inverted?”
2. Do neutrino oscillations violate CP symmetry?
3. What is the “octant” of θ_{23} ?



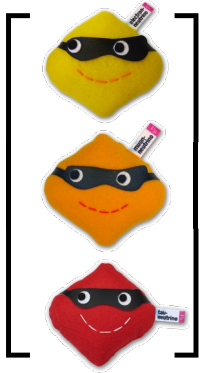
Matter effects also introduce opposite neutrino-antineutrino effects.

1. Is the mass hierarchy “normal” or “inverted?”
2. Do neutrino oscillations violate CP symmetry?
3. What is the “octant” of θ_{23} ?



The octant creates the *same* effect in neutrinos and antineutrinos.

So, what do we know?



So, what do we know?

$$\begin{bmatrix} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{bmatrix} = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \begin{bmatrix} \text{Yellow} \\ \text{Yellow} \\ \text{Yellow} \end{bmatrix}$$

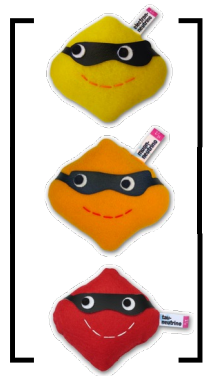
The equation illustrates the transformation of a vector of three distinct neutrino flavors (Yellow, Orange, Red) into a vector of three identical neutrino flavors (Yellow, Yellow, Yellow) through a sequence of three rotations: $R(\theta_{12})$, $R(\theta_{13}, \delta_{CP})$, and $R(\theta_{23})$.

So, what do we know?

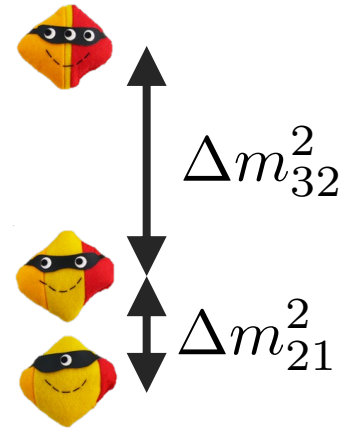
$$\left[\begin{array}{c} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{array} \right] = R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12}) \left[\begin{array}{c} \text{Yellow} \\ \text{Orange} \\ \text{Red} \end{array} \right]$$

Δm_{32}^2
 Δm_{21}^2

So, what do we know?



$$= R(\theta_{23}) \cdot R(\theta_{13}, \delta_{CP}) \cdot R(\theta_{12})$$

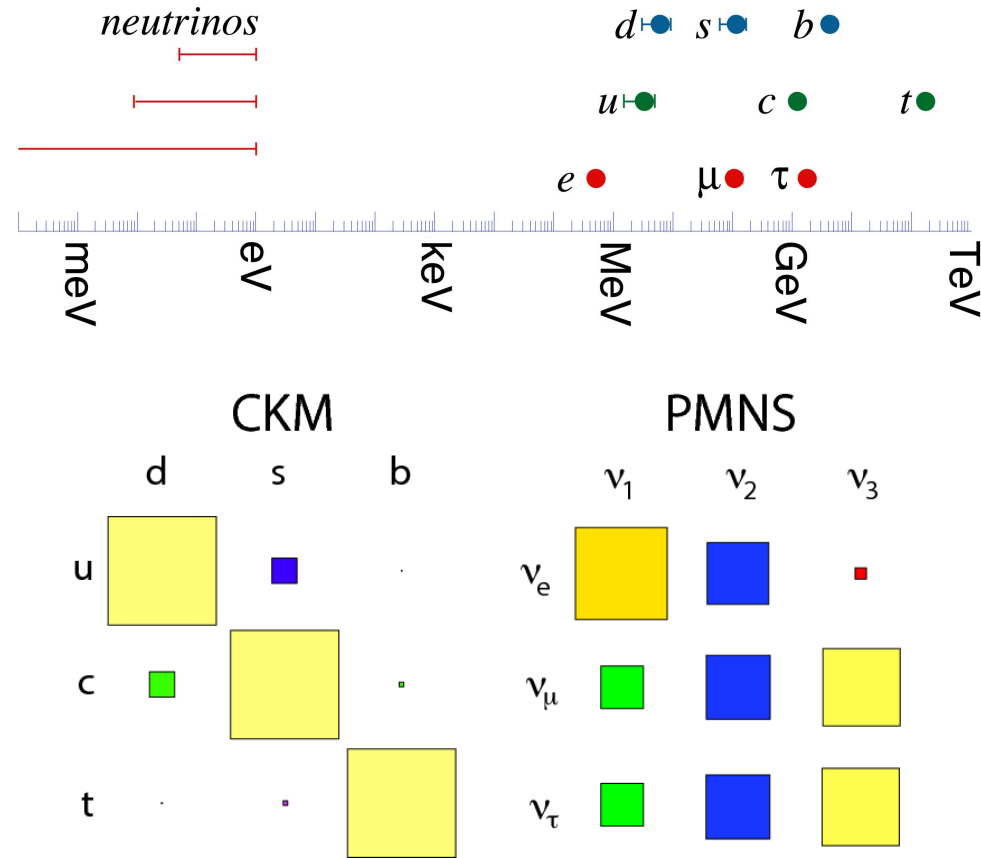


parameter	best fit $\pm 1\sigma$	3σ range	relative 1σ uncert
Δm_{21}^2 [10^{-5}eV^2]	$7.55^{+0.22}_{-0.20}$	6.98–8.19	2.7%
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (NO)	$2.51^{+0.02}_{-0.03}$	2.43–2.58	1.0%
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (IO)	$2.41^{+0.03}_{-0.02}$	2.34–2.49	1.0%
$\sin^2 \theta_{12}/10^{-1}$	3.04 ± 0.16	2.57–3.55	5.4%
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.64^{+0.15}_{-0.21}$	4.23–6.04	3-4%
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.64^{+0.15}_{-0.18}$	4.27–6.03	3-4%
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.20^{+0.05}_{-0.06}$	2.03–2.38	2.6%
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.20^{+0.07}_{-0.04}$	2.04–2.38	2.6%

From M. Tórotola at NEUTRINO2024 last week

What are we still trying to learn?

- The neutrino mass
 - ...and why it's so small
 - But oscillations can't answer those questions.
- The ordering of the neutrino masses.
 - Are they like the rest of the particles or not?
- Whether neutrinos violate CP symmetry.
- Why neutrino mixing is so different from quark mixing.



PoS (ICHEP2012) 033